Dynamic Effects of an Economic Partnership Agreement: Implications for Senegal*

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Abstract  
In this paper, I use a dynamic recursive computable general equilibrium to evaluate, for the economy of Senegal, the dynamic effects of an economic Partnership Agreement between West African countries and the European Union. In the simulations, the liberalization scheme is designed to mirror the interim agreement signed by Côte d’Ivoire and Ghana. The effects described are the shifts from the baseline numbers. I find that the production of agricultural goods will decrease, affecting employment negatively, particularly unskilled labor, since this sector is very labor intensive. In fact, employment drops by around 0.2 percent a year during the simulation period (2012-2030). GDP grows on average by 1.9 percent a year. The effects of the economic partnership agreement closely mirror the results of a free trade agreement between Senegal and the European Union, implying that a customs union between West African countries is not necessary to reap the benefits of the EPA for Senegal. The directions of these effects are stable when we use higher elasticities, or different closure rules.

1 Introduction  
West African countries and the European Union (EU) are a step closer to establishing a new framework for their trade relationship: an economic partnership agreement (EPA), consistent with the rules of the World Trade Organization (WTO). Senegal, like all least-developed countries (LDCs), exports duty-free to the EU under the everything-but-arms initiative (EBA). In the new framework, the relationship would be reciprocal, that is, the EU would benefit from the same preferred treatment in all West African countries. In addition, the EU has made the creation of a customs union between West African countries a condition for the establishment of the EPA. The effects of these policy changes on the domestic economies of the West African countries will be important and are, in fact, the primary concerns in the EPA negotiations.

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The objective of this paper is to evaluate, for the economy of Senegal, the dynamic effects of an EPA between West African countries (WA), composed of ECOWAS members\(^1\) plus Mauritania, and the EU. Two types of models are used for this type of analysis: partial equilibrium (PE) and computable general equilibrium models (CGE).

Partial equilibrium models are used when the analysis is not extended to the entire economy, but focuses on changes in specific markets after a policy change, or a shock. These models, however, by ignoring the interdependence that exists among different markets, are missing the spillover effects of shocks affecting a specific market. General equilibrium models fill this gap by describing the entire economic system, capturing not only the direct impact of a shock in a particular sector, but also the impact on other areas of the economy and the feedback effects from these to the entire economy. Two types of CGE models are commonly used: Static CGE (SCGE) and dynamic CGE (DCGE).

SCGE are used to compare the equilibrium state of an economy before and after a perturbation, when all adjustments have taken place. This type of model is widely used, and similar questions on Senegal have been studied using it. For instance, Dumont \textit{et al.} (2000) studied the impact of public infrastructure on competitiveness and growth in Senegal. They found that when public infrastructure is financed using aid, the production of non-tradables increases, but GDP decreases compared to the baseline scenario; and if financed using foreign savings, it has a positive impact on GDP. Diagne \textit{et al.} (2007), in another study on Senegal, found that trade liberalization worsens poverty and inequality in the short run and decreases production both in protected agriculture and industrial sectors. In the long run, however, it brings substantial decreases in poverty, even though income distribution worsens. SCGE models have been also used for multi-countries analysis. Decaluwe \textit{et al.} (2001) evaluated the effects of a customs union between country members of the West African Economic and Monetary Union (UEMOA) using a multi-country CGE model; the reform is shown to be welfare-improving, and has a positive impact on regional and non-regional trade flows; however, it induces negative effects on government finances.

For the Common Market of Eastern and Southern Africa, Karingi \textit{et al.} (2005) found that

\(^1\)ECOWAS member states: Benin, Burkina Fasso, Cape Verde, Cote d'Ivoire, Ghana, Guinea, Guinea Bissau, Liberia, Mali, Niger, Nigeria, Senegal, Sierra Leone, The Gambia, and Togo
an EPA with the EU leads to a steady increase in imports into member countries, and if reciprocity is not applied there is a net improvement in welfare, though the trade balance continues to fall. Under free trade, however, GDP grows at 3.4% and the trade balance improves.

The second type of model, DCGE, is receiving growing attention from researchers. In trying to capture the evolution of an economy from one equilibrium to a new one after a shock, DCGE models push the analysis further. The simulated counterfactual paths of the economy, with and without shocks, give an idea of the time paths of the likely impacts of the policy changes, and thus could serve as guidance for a better policy choice. In this line of research, Löfgren et al. (1999) analyzed the impact of the Association Agreements with the European Union on households in Morocco. The authors used a dynamic CGE model and found that removing tariffs and non-tariff barriers result in a growth slowdown in agricultural sectors, and growth in non-agricultural sectors. There are also few studies on Senegal using these models. Dissou (2002) analyzed the dynamic effects of a customs union between member countries of the West African Economic and Monetary Union on Senegal, using an intertemporal DCGE. He found that, if adopted with an outward-looking strategy, the customs union is welfare-improving for Senegal. Annabi et al. (2005) analyzed the effects of trade liberalization on welfare and poverty in Senegal. Their results indicate small negative impacts in terms of welfare and poverty, in the short run. In the long run, however, they find positive impacts on production in the industrial and services sectors, and a substantial decrease in poverty.

In this paper, I use a recursive DCGE to analyze the effects of an EPA between the EU and ECOWAS on Senegal’s economy. I find that, in the period covered by the simulation (2012-2030), the EPA increases employment by 0.3 percent, much of which is composed of skilled workers; however, in the first decade after the EPA is implemented, total employment decreases by 0.2 percent, mainly due to reduced demand for unskilled labor. This result comes from the adverse effects on sectors that are major providers of unskilled employment, such as agriculture, commerce, and public services.

The rest of the paper is organized as follow: section 2 discusses the context of the EPA and gives some background information on Senegal’s economy; in section 3, I present
the model; the data and calibration issues are dealt with in the section 4; and finally, the different simulations are explained, and the results presented and discussed in section 5.

2 Context and Economic Background

2.1 Context of the EPA

The Most Favored Nation (MFN) clause of the World Trade Organization (WTO) was established to prevent countries from giving preferential treatment a few countries while excluding the rest of the world. However, developed countries have thought of using trade as a development tool in their relationships with developing countries. This issue brought the idea of the Generalized System of Preferences (GSP), first discussed in 1968 by UNCTAD, before being adopted by the GATT in 1971 for a 10-year period, and extended permanently in 1979 with the enabling clause.

A waiver to the MFN rule, the GSP gives developed countries legal grounds to treat their trading partners differently, depending on their level of development. However, this waiver is constrained to be non-discriminatory among developing countries, and non-reciprocal. Regarding these two conditions, the European Union (EU) - African Caribbean and Pacific (ACP) relationship violates not only the reciprocity clause on FTA (Article XXIV of the GATT on free trade agreements), but also goes against the underlying principle of the GSP, that is the non-discrimination clause. Because, first, ACP’s imports from the EU are subject to trade barriers, while they export to the EU under the GSP; and second, only the developing ACP countries are beneficiaries.

With the complaints of the excluded developing countries and pressure from the WTO, the EU is engaged in the process of bringing its trade relations with the ACP countries into conformity with the WTO rules; this process formally started with the Cotonou agreements in 2000. In September 2002, the EU and different groups of ACP countries, including the Economic Community of West African Countries (ECOWAS) and Mauritania, established a new framework for their trade relationship, the economic partnership agreements (EPA), to conform to the rules of the WTO. In this new relationship, trade between West African countries and the EU will be free; the latter will ease up all trade barriers, while the former
will drop all tariffs on at least 70 percent of its imports from the EU. The negotiations were expected to be completed by January 2008; however, the deadline was reached without a final agreement, except between the EU and the CARIFORUM\textsuperscript{2}. Many countries have, individually or as subgroups, signed interim agreements, but still remain within their groups for the final EPA negotiations.

ECOWAS represents the biggest trading partner of the EU within the ACP group, with around 40 percent of imports and 32 percent of exports, and as of yet has not reached a final agreement on the EPA with the EU. However, two members, Côte d’Ivoire and Ghana, have signed interim agreements with the EU, in March 2009 and November 2008, respectively. Nigeria is trading under the GSP standard, and Cape Verde (until 2011) and the LDCs of the group are trading with the EU under the Everything But Arms (EBA) initiative.

Benefiting from the EBA initiative Senegal has duty-free access to the EU market; therefore, it has no apparent reason for joining an agreement to have an access it already has. However, it is widely agreed that the benefits from trade go beyond access to a wider market for domestic producers; in fact, if most domestic firms can access a larger market by exporting duty free to the EU, the domestic economy will miss most of the benefits attributed to trade openness such as lower prices for intermediate inputs and consumer goods, technology transfer, and efficiency gains through competitive exposure of domestic firms. However, the costs in terms of unemployment, factor incomes, and loss of revenue for the government, during the transition period play a major role in the negotiations. Economists in general agree on the long-term benefits, but the path that the economy takes during the transition period is unclear and remains the main concern of developing countries when negotiating RTAs with more-developed countries.

\subsection*{2.2 Senegal’s Trade Policies and Trade Agreements}

Senegal is a founding member of the Economic Community of West Africa (ECOWAS). This body, established in 1975, is aimed at unifying the markets of the member countries and harmonizing their trade policies and ultimately at creating an economically-integrated

\textsuperscript{2}CARIFORUM countries: Antigua and Barbuda, Bahamas, Barbados, Belize, Dominica, the Dominican Republic, Grenada, Guyana, Haiti, Jamaica, Saint Lucia, Saint Vincent and the Grenadines, Saint Christopher and Nevis, Suriname, and Trinidad and Tobago.
entity. A revision was undertaken in 1993 to revive the economic integration project. The trade liberalization scheme adopted categorizes trade into three groups. The first two groups, made up of unprocessed goods, and traditional handicraft products, was granted an immediate and full liberalization status. The third group, made up of industrial goods, would be liberalized gradually over the 1990 to 2000 period. Tariffs are still high within ECOWAS and most of the deadlines were not met. However, efforts to bring the rates down and transform ECOWAS into a unified market are real, especially in the wake of an EPA between ECOWAS and the EU. In 1994, a subgroup of countries within the ECOWAS, the West African Economic and Monetary Union (UEMOA\textsuperscript{3}), signed the UEMOA treaty, and in 1996 a preferential tariff regime was enforced among member states.

Senegal's trade policies are tailored to fit the UEMOA's common external tariff (CET) adopted in 1997. UEMOA's CET defines four major bands for customs duties. Products admitted in the first band are admitted duty free. The approved products are mainly pharmaceuticals (drugs and other medicines for infectious diseases such as HIV/AIDS), agricultural inputs, capital goods, computer and data processing equipment not available through local production, and social, cultural, and scientific goods. Raw materials, crude oil, and cereals for industries are subject to a 5 percent tariff rate, which corresponds to the second band. The third band, corresponding to a 10 percent tariff, is applied to semi-finished products, diesel and fuel oil, intermediate goods, and other cereals. The last band of 20 percent is imposed on final consumption goods, capital goods, and computer and data processing equipment already available through local production, as well as new and used vehicles. In addition to the CET, however, Senegal applies supplementary levies in conformity with UEMOA policies, and taking into account all levies, the average applied duties are higher than if the CET alone were applied.

For products of UEMOA origin, a preferential regime is applied. Since 2000, duty free access is granted to all agricultural products and handicraft goods and for approved industrial products. Eligible manufactured goods must have at least 60 percent of the raw materials or 40 percent of the added value of UEMOA origin. For products not approved,

\textsuperscript{3}UEMOA member states: Benin, Burkina Fasso, Cote d'Ivoire, Guinea Bissau, Mali, Niger, Senegal, and Togo
a 5 percent reduction is granted. And effective January 1st, 2000, approved industrial and agricultural products within UEMOA may be imported free of customs duty.

Beside the ECOWAS and the UEMOA agreements, Senegal has also been a member of the GATT since September 1963, and later of the WTO. The country has a long history of trade relationships with the EU, its greatest trade partner, under the EU-ACP relations. Admitted to the group of LDCs in April 2001, Senegal has the opportunity to export duty free to the EU.

The new challenge now goes beyond the UEMOA and ECOWAS treaties, because a customs union between WA countries is put as a condition for the EPA with the EU; but this status is yet to be met. However, since January 2006, a CET was adopted and scheduled for application on January 2008. The West African CET is an extension of the UEMOA CET, organizing trade into four bands as set out above. Under the proposition of Nigeria, a fifth band of a 35 percent tariff rate was adopted on June 2009 to protect new industries.

When the EU-WA negotiations end, the EPA will be the framework that defines the trade relationship between Senegal, the rest of the WA countries, and the EU. The EU will abolish all trade restrictions (tariffs and non tariffs) on its imports from the ACP countries, while the latter will liberalize up to 70 percent of imports from the EU, with the possibility of a gradual phasing out of tariffs. By the end of 2007, when it became clear that the EU-WA EPA would not be completed, Côte d’Ivoire and Ghana concluded interim agreements with the EU "to prevent trade interruption". Côte d’Ivoire signed the interim agreement in November 2008; Ghana is yet to sign its agreements, however, the first phase has been in effect since January 2009. From that period until now, the negotiations have been ongoing, with a cycle of propositions and rejections revolving around two main issues: the extent of liberalization on the WA countries side, and the level of aid attached to the development dimension of the EPA on the EU side. The WA countries’ last offer was a 67 percent liberalization over 25 years, on October 2009, and they are yet to respond to a 70 percent liberalization at a higher speed proposed by the EU. The EU, on its side, committed to spend €6.5 billion over a five-year period, on May 2010.
2.3 Economic Background

The Senegalese economy grew at 4.2 percent on average during the 2000-2007 period, but was affected by the slowdown of the global economy in 2008 and 2009, with 2.3 and 1.2 percent growth rates, respectively (Table 2.1). The primary sector (agriculture, fishing, and mining), 13.5 percent of GDP and the main provider of employment, grew at 1.4 percent in the 2000-2009 span; services, representing around two thirds of GDP, grew at 4.5 percent; and finally manufacturing, accounting for 20 percent of GDP, grew at 3.4 percent. Available resources come from domestic production (77.6 percent), imports (16.6 percent) and taxes (5.8 percent). Consumption, intermediate and final goods, represent, respectively, 36 and 41 percent of total expenditures; investment and exports account for 11 and 12 percent, respectively. Investment grew at the average rate of 6 percent during the same time period; both final and intermediate consumption recorded a 4 percent growth rate (ANDS 2004).

Table 2.2 shows the tariff rates on imports to and from Senegal. Tariff rates on imports from West African countries (10.3 percent) are on average lower than the rates on imports from the EU and the rest of the world (12.4 percent).

The import-GDP and export-GDP ratios remained very stable, with an average of 36.4 and 27.2 percent respectively. In 2008, capital and intermediate goods (not including raw materials) represented around 39 percent of Senegalese imports, consumption goods accounted for 39 percent, and raw materials 22 percent; on the export side, these numbers were, respectively, 44 percent, 38 percent and 18 percent. The country’s two main trading partners are the EU, and the West African countries. The EU, for instance, provided around 75 percent of the total imports in capital and intermediate goods and 50 percent of the consumption goods. On the export side, however, Sengal trade mostly raw materials with the EU, the latter receiving around 60 percent of Senegal’s total exports in that group of commodities. On the other hand, WA countries represent the main source of raw materials for Senegal, constituting 55 percent of the total imports of raw materials; while they received 45 percent of Senegalese exports of capital and intermediate goods, and 84 percent of its exports of consumption goods.

The EPA, by creating a customs union among WA, will on the one hand remove all trade
restrictions among WA countries, and on the other hand, will liberalize trade "substantially" between Senegal and the EU. Senegal is a small country, not only economically, but also geographically. The latter, added to the fact that agriculture, in Senegal, mainly depends on rainfall, indicate that the country has no real comparative advantage in agriculture compared to, not only WA countries, but also some EU counties like France, which are relatively more endowed in land. In the primary goods subgroup, however, the country is relatively more endowed in the production of fish. Further, the pattern of trade with WA countries shows that Senegal’s comparative advantage compared to these countries lies in light manufacturing, such as food processing, for instance.

In such a setting, under the EPA, we would expect the imports of agricultural goods to increase, while production and exports go down. The production and exports of fish, on the other hand, is expected to increase. As for manufactured goods, the production of light manufacturing, food processing and the like, is expected to go up. Imports of capital and intermediate goods, from the EU particularly, would increase when tariffs are removed or decreased; from WA countries, we would expect the imports of raw materials to go up.

Agriculture occupies more than 60 percent of the labor force in Senegal. The expected negative effects on the production of agricultural goods would, by extension, negatively affect the level of employment in Senegal; these negative effects more or less would be countered by the increase in the production of fish, and in the long term by the increase in the production of light manufacturing.
Table 2: Import tariffs (simple average)

<table>
<thead>
<tr>
<th></th>
<th>On imports from regions</th>
<th>On imports from Senegal</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>WA</td>
<td>EU</td>
</tr>
<tr>
<td>Agriculture</td>
<td>5.70</td>
<td>10.70</td>
</tr>
<tr>
<td>Mining</td>
<td>7.60</td>
<td>7.70</td>
</tr>
<tr>
<td>Wood</td>
<td>13.60</td>
<td>14.10</td>
</tr>
<tr>
<td>Rubber</td>
<td>10.10</td>
<td>10.70</td>
</tr>
<tr>
<td>Fishing Products</td>
<td>5.00</td>
<td>10.10</td>
</tr>
<tr>
<td>Processed food</td>
<td>8.60</td>
<td>16.00</td>
</tr>
<tr>
<td>Leather</td>
<td>14.70</td>
<td>14.70</td>
</tr>
<tr>
<td>Textile</td>
<td>17.40</td>
<td>18.40</td>
</tr>
<tr>
<td>Tobacco</td>
<td>4.90</td>
<td>9.70</td>
</tr>
<tr>
<td>Beverage</td>
<td>10.20</td>
<td>19.40</td>
</tr>
<tr>
<td>Chemicals</td>
<td>9.00</td>
<td>9.50</td>
</tr>
<tr>
<td>Petroleum and Coal</td>
<td>4.30</td>
<td>4.40</td>
</tr>
<tr>
<td>Transport Equipment</td>
<td>9.40</td>
<td>9.00</td>
</tr>
<tr>
<td>Glass and Pottery</td>
<td>15.70</td>
<td>16.20</td>
</tr>
<tr>
<td>Iron and Steel</td>
<td>13.10</td>
<td>13.60</td>
</tr>
<tr>
<td>Machinery</td>
<td>12.50</td>
<td>12.70</td>
</tr>
<tr>
<td>Paper</td>
<td>6.40</td>
<td>6.80</td>
</tr>
<tr>
<td>Other products</td>
<td>18.00</td>
<td>19.00</td>
</tr>
</tbody>
</table>

Source: International Trade Center (ITC)

Figure 1: Import-GDP and export-GDP ratios

Source: Agence national de la demographie et de la statistique (ANDS)
3 Description of the Model

The settings of the model are presented in this section. It is a recursive dynamic CGE model of a small open economy, based on that of Thurlow (2004), which also is an extension of the model in Lofgren et al. (2002). It differs from these models in that each activity produces only one commodity, and in other settings (parameters) that are discussed in the next section. The model has two main components. The first one is the static module, which consists of the core equations of the model; the calibration of this part defines the values of the different parameters, offers the starting values for the endogenous variables, and solves for the values of the endogenous variables within each period. The dynamic module defines the equations linking the different periods. The equations of the model consist of the first-order conditions of the different optimization programs of institutions, along with the constraints, and the different accounting equations. They are presented in the appendix.

3.1 Static Module

The static part of the model identifies 28 activities, each producing one commodity, and counts four institutions: households, enterprises, the government, and the rest of world. The model separates activities from commodities, the former are the domestic production units, while the latter, similar to the domestic markets, buy goods from domestic and foreign producers, and allocate it between the domestic sales and exports. Households consume home and imported goods to maximize their inter-temporal utility; firms maximize their profit in a constant return to scale (CRS) framework; the government collects taxes to consume and make transfers; and they all have access to the international capital market where they can lend and borrow at the world interest rate.

3.1.1 Activities

Activities correspond to domestic producers; they use three factors of production, unskilled and skilled labor, and capital to produce goods and services. Primary factors of production (capital and labor) are combined in a CES function to get value added (VA); aggregate
intermediate input is a Leontief function of disaggregated intermediate inputs. Activity output is a Leontief function of intermediate inputs and VA, the intuition being that the optimal combination between VA and intermediate inputs is defined by technology rather than by the decision of a manager (Thurlow, 2004). Firms produce the quantities that maximizes their profits, subject to a production technology constraint:

\[
PROFIT = (1 - t_a) P_a Q_a - \sum_c P_{qc} Q_{int_a c} - \sum_f W_{f f d} d_{fa} Q_{f f} 
\tag{1a}
\]

\[
Q_v_a = \alpha v_a \left( \sum \delta_{fa} Q_{f a}^{\mu_{fa}} \right)^{-\frac{1}{\mu_{fa}}} \tag{1b}
\]

\[
Q_a = \text{Min} \left[ \frac{Q v_a}{iv_a}, \frac{Q l_a}{it_a} \right]. \tag{1c}
\]

\[
Q_{int_a c} = i c_{a c} Q l_a \tag{1d}
\]

\[
P_{int c} = \sum_c P_{qc} i c_{ca}. \tag{1e}
\]

Where \( P_a \) is the activity price of the commodity produced by activity \( a \); \( Q_a \) is the quantity of commodity produced by activity \( a \); \( P_{qc} \) is the price of composite commodity \( c \), which is a mixture of home produced and imported goods; \( Q_{int_a c} \) is the quantity of commodity \( c \) as intermediate to activity \( a \); \( W_{f f} \) is the average price of factor \( f \); \( d_{f a} \) is a wage distortion factor for factor \( f \) in activity \( a \); \( Q_{f f} \) is the quantity of factor \( f \); \( Q v_a \) is the quantity of value added; \( i c_{a c} \) is the quantity of commodity \( c \) per unit of aggregate intermediate input; \( Q l_a \) is the quantity of aggregate intermediate input; \( iv_a \) is the quantity of value added per unit of activity; \( it_a \) is the quantity of aggregate intermediate input per unit of activity.

Once produced, firms allocate their output between domestic and foreign markets by maximizing their total revenue in both markets. The quantities of domestically produced commodities are a constant elasticity of transformation function of domestic sales and exports. As the relative price of the goods changes, the producer increases slightly the quantity sold in one market relative to the other.
3.1.2 Consumers

The model considers one category of households, deriving their income from factors of production, and transfers from the government and the rest of the world, and using it to pay taxes, to consume, and to make transfers to the rest of the world; the residual income is saved. They consume composite commodities which are also used for investment and for intermediate inputs. Households’ demand for a commodity is derived by maximizing their total utility. The consumers’ preferences are represented by a Stone-Geary utility function:

$$U = \prod_c (Q_c - \gamma_c)^{\beta_c}.$$  

(2)

Households maximize their utilities under the constraint that total expenditures equal total incomes. The solutions give the demand and expenditure functions in equations 7 and 8 respectively.

$$Q_c = \gamma_c + \frac{\beta_c}{P_{qc}} \left( EH - \sum P_{qc} \gamma_c^m \right).$$  

(3a)

$$P_{qc} Q_c = P_{qc} \gamma_c + \beta_c^m \left( EH - \sum P_{qc} \gamma_c^m \right).$$  

(3b)

Where $Q_c$ is the quantity of commodity $c$ consumed by household; $\gamma_c$ is the subsistence consumption of marketed commodity $c$ for household; $\beta_c^m$ is the marginal share of consumption spending on marketed commodity $c$ for household; and $EH$ is the consumption spending of households.

Composite commodities are CES aggregations of domestic goods and aggregate imports, allowing for imperfect substitution between home goods and imports (Armington assumption). Households allocate their consumption expenditures between domestic and imported commodities by minimizing total costs subject to imperfect substitutability of goods from the two origins.

3.1.3 Trade

Imports are differentiated with respect to their region of origin; for each commodity, aggregate imports are a CES aggregation of imports from different regions. This specification
assumes imperfect substitutability between the goods imported from different regions, de-
pending on their relative price. A similar treatment is applied to exports, with aggregate
exports being a CES function of exports to different regions. The regional disaggregation
allows for different tariff rates for different regions making the analysis of preferential tariffs
between regions more practical.

Transaction costs are incurred on domestic sales, imports, and exports, as fixed shares
per unit of commodity. Exports and imports prices include transaction costs and are ad-
justed for any applied tax (import tariffs or export taxes). The current account balance,
corresponding to foreign saving, equals the difference between exports plus income received
from the rest of the world and imports plus income paid to the rest of the world.

3.1.4 Government

Government, in this model, is an entity separated from the public service activity; it is,
however, the primary buyer of the service produced by the latter. On one hand, it collects
taxes and receives transfers from enterprises and from the rest of the world. On the other
hand, it spends on final consumption and makes transfers to other institutions. The differ-
ence between government revenues and expenditures is the budget deficit, financed through
borrowing from domestic institutions and the rest of the world.

3.1.5 Equilibrium Conditions and Macro-closures

The solution to the model depends on how the equilibrium is reached in each market and on
a set of macro closures. Senegal is a small open economy; therefore, it faces infinitely elastic
world demands and supplies for its imports and exports at world prices. Import prices paid
by demanders include import tariffs, and the transaction costs per unit of commodity. As
for domestically supplied goods, buyers pay the producer prices plus the transaction costs.
The supply prices of exports is equal to world prices adjusted for any transaction costs and
export taxes. The supply prices of domestically sold outputs are equal to the prices paid
by domestic demanders net of transaction costs. In domestic markets, flexible prices ensure
the equilibrium between demand and supply for disaggregated commodities as well as for
composite commodities.
Labor markets’ closures depend on the type of labor and on the characteristics of the market. Globally, unemployment rate is around 13 percent and prevails in both markets. More than 100,000 newcomers enter the labor market each year, with 75,000 more jobs created between 1995 and 2004, most of which went to the informal sector, the main provider of employment in the country. Employment, in both the skilled labor and unskilled labor markets, is driven by the demand from the private and public enterprises (World Bank, 2007). In the unskilled labor market, labor supply is fixed at the observed level, the importance of unemployment dictates a fixed wage; the supply, therefore, adjusts passively to match demand. Unemployment in the skilled labor market may be explained by the fact that both workers and firms are responsive to the real wage. In this case, the latter adjusts to ensure equilibrium (Lofgran et al. 2002). To be more realistic, an exogenous wage-distortion factor is introduced to make them different across sectors. Capital is sector specific and fully employed; the equilibrium between demand and supply is ensured by a sector-specific flexible wage.

The government budget deficit equals its total revenues net of its total expenditures, which is kept fixed in real terms. Therefore, the closure of the government account depends on how the government’s saving and its total revenues, or more precisely, the tax rates are treated. In this model, the tax rates on domestic institutions are fixed; therefore, to ensure equilibrium, uniform point changes in sales taxes are applied.

Foreign savings remain fixed, which leaves the exchange rate as the adjusting variable. The opposite closure is considered in the sensitivity analysis.

Investment is financed by savings from domestic institutions and the rest of the world. With the government’s persistent budget deficit, and low level of domestic savings, an investment driven closure would be more realistic. However, instead of maintaining the investment fixed, nominal share of investment in total absorption is set fixed; this option allows investment to vary. The adjustment variables are the saving rates of households and enterprises, which receive a uniform point change to equal total investment. This closure, known as the balanced closure, is a variant of investment-driven closures; it spreads the adjustments to all components of absorption, for the shares of households and government consumptions in total absorption are also fixed. This closure is very useful in analyzing the
role of complementary policies to external shocks or policy changes (Lofgran et al. 2002).

3.2 The Dynamic Module

The dynamic part of the model helps draw a counterfactual path of the economy in reaction to external shocks or policy changes. The dynamics are carried by a certain number of factors, which are adjusted between periods to account for some non-policy related changes in some variables or parameters in the model. Those changes concern the population growth, changes in the labor force, capital accumulation and government expenditure.

Population growth enters the model through the demand for goods and services of households, by increasing private consumption spending on each commodity (equations 2.4a and 2.4b) for households. Equation 2.4a represents a linear expenditure system (LES) specification of the demand; it allows for an income-independent level of consumption ($\gamma_c$) and a linear relationship between consumption and disposable income. Population growth affects households’ spending by increasing the income-independent parts of households’ demands for commodities ($\gamma_c$) at the same rate as the population growth. This change, however, does not affect consumption at the margin but on the average, which means new consumers have the same preferences as the existing ones.

For the two types of labor distinguished in the model, skilled and unskilled labor, the dynamic depends on the closure adopted in each market. In the unskilled labor market, the closure adopted assumes an infinitely elastic labor supply, therefore, no adjustment is necessary in this factor market. In the skilled labor market, the supply is endogenous, making any exogenous adjustment unnecessary.

Capital accumulation is endogenous in the model. Each period’s capital stock is a function of the previous period’s capital stock and investment spending. In the model, capital renewal motion starts by allocating the new capital across sectors. This process starts by defining first the share of each sector in the new capital. Equation 2.5 defines the average rental rate of capital.

$$Aw_{ft} = \sum_a \left[ \left( \frac{Q_{fat}}{\sum_a Q_{fat}} \right) W_{ft}, W_{f \text{dist}_{fat}} \right]$$

(4)
Where \( Q_{f,a,t} \) is the quantity demanded of factor \( f \) from activity \( a \) in time period \( t \); \( Aw_{f,t} \) is the average capital rental rate in time period \( t \); \( W_{f,t} \) is the average price of factor \( f \); and \( W_{fdist,f,a,t} \) is a wage distortion factor for factor \( f \) in activity \( a \). The share of new capital for each sector \( (\eta_{f,a,t}^\alpha) \) is estimated using equation 2.6. For \( \frac{W_{f,t}W_{fdist,f,a,t}}{Aw_{f,t}} > 1 \), the second term on the right hand side is greater than 1 and the converse is true if \( \frac{W_{f,t}W_{fdist,f,a,t}}{Aw_{f,t}} \leq 1 \). 

\[ \beta^\alpha \] is the intersectoral mobility of investment parameter; if its value is zero, the new capital share of the activity is the same as its share in the existing capital. Sectors with a rental rate of capital higher than the average receive a share of new capital higher than their share of existing capital.

\[
\eta_{f,a,t}^\alpha = \left( \frac{Q_{f,a,t}}{\sum_a Q_{f,a,t}} \right) \left[ \beta^\alpha \left( \frac{W_{f,t}W_{fdist,f,a,t}}{Aw_{f,t}} - 1 \right) + 1 \right] \quad (5)
\]

To get the new capital for activity \( a \) \( (\nabla K_{f,a,t}^\alpha) \), the gross fixed capital formation is first deflated by the price of capital \( (P_{k,f,t}) \) and multiplied by the sectoral share of new capital, as displayed in equation 2.7a. From there, the perpetual inventory method is used to determine the capital stock of each sector in period \( t \).

\[
\nabla K_{f,a,t}^\alpha = \eta_{f,a,t}^\alpha \frac{\sum_c P_{q_{c,t}}Q_{inv_{c,t}}}{P_{k,f,t}} \quad (6a)
\]

where,

\[
P_{k,f,t} = \sum_c P_{q_{c,t}} \frac{Q_{inv_{c,t}}}{\sum_c Q_{inv_{c,t}} \quad (6b)}
\]

### 4 Data and Calibration

The model is calibrated using the 2004 social accounting matrix for Senegal (Cissokho, 2010). Besides the SAM, data on some other parameters, necessary to the dynamics of the model, have been collected from similar work on Senegal. Those parameters include the elasticities of substitution between primary factors of production, between domestic and imported commodities, and between different commodities by households; further, data are provided on shares of regional imports, and exports and tariff revenues from the different regions considered in the model.

Elasticities of substitution are selected from various studies on Senegal (Dumont and
Mesplé-Somps, 2000; Diagne et al., 2003). The Armington elasticities (Table 2.3) assume imperfect substitutability between domestically produced and imported goods; lower elasticities indicate greater differences between domestic and imported goods; therefore, changes in relative prices of imports and home goods bring slight changes in the allocation of expenditures between domestic and imported goods. The elasticities of substitution between primary factors serve in the CES aggregation of capital and labor. The elasticities of substitution between commodities by households are from the GTAP African database.

Imports, exports, and tariff revenues are regrouped by region; the shares of each region, by commodity, are computed using data from the world integrated trade solution (WITS). Employment numbers are given in the input-output table from the statistical agency of Senegal; the disaggregation into skilled and unskilled labor is realized using information from the ESAM II (households survey in Senegal, 2003). The initial capital in the model is generated using the capital-output ratio; these numbers at the sectoral level, are collected in Estache and Muñoz (World Bank, 2007). The depreciation rate used in this model for manufactures is of the same magnitude as in most studies on Senegal, 5 percent (Diagne et al, 2003,2007 and Dissou, 2003); however, for services I use a rate of 3 percent. With respect to these last two characteristics, this paper differs from the previous papers (Thurlow, 2004, Diagne et al., 2003,2007 and Dissou, 2003).

5 Simulations and results

5.1 Simulations

The interim agreements between the EU and Côte d’Ivoire set the liberalization process and scope as follows: up to 2012, 58.5 percent of imports from the EU will be liberalized; between 2013 and 2017, 10.6 percent; and finally between 2018 and 2022, 9.9 percent. On the Ghanian side, the import liberalization agenda is set as 28.8, 42.6 and 8.3 percent, corresponding, respectively, to the time periods defined for Côte d’Ivoire. Values are with respect to the 2004-06 imports for each country. Trade, under the interim agreements, is regrouped into four main bands, A, B, C, and D. The first three bands are liberalized progressively and successively as follows: band A, up to 2012; band B, between 2013 and
Table 3: Armington elasticities

<table>
<thead>
<tr>
<th>Commodities</th>
<th>SIGMA</th>
<th>Commodities</th>
<th>SIGMA</th>
</tr>
</thead>
<tbody>
<tr>
<td>agriculture</td>
<td>2.62</td>
<td>Telecommunication</td>
<td>0.3</td>
</tr>
<tr>
<td>Mining and extracting</td>
<td>1.6</td>
<td>Restaurants and Hotels</td>
<td>0.3</td>
</tr>
<tr>
<td>Wood</td>
<td>1.5</td>
<td>Glass and Pottery</td>
<td>1.5</td>
</tr>
<tr>
<td>Rubber</td>
<td>1.5</td>
<td>Iron and steel</td>
<td>1.3</td>
</tr>
<tr>
<td>fishing</td>
<td>1.2</td>
<td>Machinery</td>
<td>1.3</td>
</tr>
<tr>
<td>Food processing</td>
<td>2</td>
<td>Construction</td>
<td>0.3</td>
</tr>
<tr>
<td>Leather</td>
<td>1.5</td>
<td>Paper products</td>
<td>1.5</td>
</tr>
<tr>
<td>Textile</td>
<td>1.5</td>
<td>Other Products</td>
<td>1.5</td>
</tr>
<tr>
<td>Tobacco products</td>
<td>1.5</td>
<td>Commerce</td>
<td>0.3</td>
</tr>
<tr>
<td>beverages</td>
<td>2</td>
<td>Transportation</td>
<td>0.3</td>
</tr>
<tr>
<td>Chemicals</td>
<td>1.3</td>
<td>Real estate</td>
<td>0.3</td>
</tr>
<tr>
<td>Electricity, Gas and water</td>
<td>0.3</td>
<td>Public Services</td>
<td>0.3</td>
</tr>
<tr>
<td>petroleum and coal</td>
<td>0.3</td>
<td>Financial services</td>
<td>0.3</td>
</tr>
<tr>
<td>Transport equipment</td>
<td>1.3</td>
<td>Other Services</td>
<td>0.3</td>
</tr>
</tbody>
</table>

Source: Dumont and Mesplé-Somps, 2000; Diagne et al., 2003.

2017; and band C, between 2018 and 2022. The last band is excluded from liberalization; the selected products or sectors are the sensitive ones, based on their fragility or on their importance in fiscal revenue collection for the government. Even if the EPA contents are likely to be different from the agreement signed by Côte d'Ivoire and Ghana, the progressive and successive liberalization scheme will be maintained. The simulations, in the different scenarios considered in this paper, are designed in a similar way.

I have considered five simulation cases: The baseline, corresponding to the scenario without any shock; FTAEU, corresponding to the case which Senegal forms a free trade area with the European Union; FTAWA, in which the West African countries form a custom union; FTAEPA, in which the West African countries and the European Union form an economic partnership agreement; and FTAWORD, in which Senegal engages in free trade with the rest of the world.

The baseline is the scenario without any change in trade regime; it traces a counterfactual path for the economy that serves as a benchmark for comparison for all remaining scenarios. Shifts from the results in this simulation represent the effects of the shock introduced in each of the remaining cases.

The second scenario assumes an FTA between Senegal and the EU. Senegal, being a
least-developed country, exports to the EU duty free under the EBA; therefore, any trade liberalization between the two countries affects only the tariffs on Senegalese imports from the EU. Following the example in the interim agreements, I have regrouped the different commodities in four bands. The first band, A, regroups machineries and appliances, iron and steel, transport equipment, wood, tobacco, leather, and fishing. The second band, B, is made up of glass and pottery, textiles, beverages and mining. The third band, C, comprises rubber, petroleum, chemicals and other products; and the last band, D, includes agricultural goods, paper, and processed food. Band D is excluded from liberalization, and represents 28 percent of Senegal’s imports from the EU in 2004, leaving 72 percent of imports to be liberalized; the negotiations are planning a 70 percent cut in tariffs on WA countries’ imports from the EU. A gradual and successive liberalization of the different bands is set up in the simulation; each band is liberalized within a six-year period, and for each band the liberalization starts with a drop of 50 percent in tariff rates; a gradual decrease of 10 percent is then applied until trade is completely free at the end of the corresponding period. In this paper, the liberalization of the different bands is implemented during the following time period: 2012-2017 for band A; 2017-2022 for band B; and 2022-2027 for band C. The tariff removal starts with less-sensitive sectors and then moves to the more-sensitive ones, in terms of fiscal revenues and employment.

The third simulation corresponds to the case of a customs union between the WA countries. In this case, the liberalization schemes for products in bands A, B and C are the same as those in FTAEU. Within band D, tariffs on agricultural products are completely removed in the first year of implementation; processed food and paper products are liberalized following the plan for band C in FTAEU. The fourth scenario, FTAEPA, the most important one in this paper, corresponds to the case of an EPA between the WA countries and the EU. The liberalization scheme here is the sum of the schemes in the FTAEU and the FTAWA. Within this scenario, trade between Senegal and the EU is set as in the FTAEU; similarly trade between Senegal and the rest of WA countries is set as in the FTAWA.

The fifth and last scenario, FTAWORLD, corresponds to a free trade between Senegal and all its trading partners; tariffs are completely removed on all trade in this case.
5.2 Results

The effects of the different scenarios are presented as shifts from the baseline numbers. Graphs 2.1-2.12 show the impacts on production, GDP, absorption, consumption, investment, employment, imports, and exports, of the different policy changes. Tables 2.1-2.4 present the average effects of the different simulations on production, imports and exports.

The import tariff revenue represents 17.3 percent of the government total revenue. The decrease or removal of tariffs will, therefore, affect the latter. In the short term, the government will have to make up the loss of revenue by using other sources. In this paper, the government’s saving is maintained fixed, as well as its share in total absorption. The adjusting variable becomes the government revenue, through point changes in sales tax rates. The effects, therefore, of policy changes in all scenarios, are revenue-neutral for the government. The effects on the government income, presented in Table 2.5, describe the differences in the evolution of public spending in the different scenarios relative to the baseline; on average, the shifts in the government income are 0.2, 0.5, and 0.7 percent over the period of simulation (2012-2030) under the West African Customs Union (FTAWA), the free trade with the EU (FTAEU) and the EPA (FTAEP), respectively. As for households their income, during the same period, has increased by 0.1, 1.4, and 1.5 percent under the FTAWA, the FTAEU and the FTAEP, respectively.

Total production, in Senegal, increases under all FTAs, with the West African Customs Union yielding the weakest impact, with 1.1 percent on average over the simulation period (2011-2030); under a free trade agreement with the EU and with the economic partnership agreement, total product increases by 2.1 and 2.2 percent, respectively; free trade, however, has the largest impact on total product, with a 10.4 percent increase on average. The increases in total production are mostly accounted for by manufacturing, except under the West African Customs Union scenario, in which increased production mainly comes from the increase in the production of primary goods. Manufacturing rises by 3.2 and 3.3 percent under free trade with the EU and under the EPA. These increases are concentrated in sectors such as transport equipment, (up 7.1 percent under FTAEU and 6.7 percent under FTAEP); iron and steel, (up 7.8 percent under FTAEU and 8 percent under FTAEP);
<table>
<thead>
<tr>
<th>Industry</th>
<th>FTAWA</th>
<th>FTAEU</th>
<th>FTAEPA</th>
<th>FTAWORLD</th>
</tr>
</thead>
<tbody>
<tr>
<td>Agriculture</td>
<td>-0.10</td>
<td>-0.50</td>
<td>-0.60</td>
<td>7.30</td>
</tr>
<tr>
<td>Mining</td>
<td>0.00</td>
<td>0.90</td>
<td>0.90</td>
<td>3.90</td>
</tr>
<tr>
<td>Wood</td>
<td>0.40</td>
<td>0.60</td>
<td>1.00</td>
<td>4.50</td>
</tr>
<tr>
<td>Rubber</td>
<td>0.10</td>
<td>3.50</td>
<td>3.60</td>
<td>19.60</td>
</tr>
<tr>
<td>Fishing</td>
<td>2.90</td>
<td>7.20</td>
<td>10.50</td>
<td>18.10</td>
</tr>
<tr>
<td>Processed food</td>
<td>0.30</td>
<td>0.30</td>
<td>0.50</td>
<td>13.70</td>
</tr>
<tr>
<td>Leather</td>
<td>-0.10</td>
<td>3.70</td>
<td>3.50</td>
<td>11.50</td>
</tr>
<tr>
<td>Textile</td>
<td>0.20</td>
<td>1.00</td>
<td>1.20</td>
<td>6.40</td>
</tr>
<tr>
<td>Tobacco</td>
<td>-0.10</td>
<td>1.50</td>
<td>1.40</td>
<td>10.10</td>
</tr>
<tr>
<td>Beverages</td>
<td>0.00</td>
<td>2.20</td>
<td>2.10</td>
<td>9.20</td>
</tr>
<tr>
<td>Chemicals</td>
<td>0.10</td>
<td>2.70</td>
<td>2.80</td>
<td>27.50</td>
</tr>
<tr>
<td>Electricity gaz and water</td>
<td>0.10</td>
<td>1.80</td>
<td>1.80</td>
<td>7.60</td>
</tr>
<tr>
<td>Petroleum and Coal</td>
<td>0.10</td>
<td>3.30</td>
<td>3.40</td>
<td>15.70</td>
</tr>
<tr>
<td>Transport equipment</td>
<td>-0.40</td>
<td>7.10</td>
<td>6.70</td>
<td>17.00</td>
</tr>
<tr>
<td>Telecommunication</td>
<td>-0.10</td>
<td>0.60</td>
<td>0.50</td>
<td>2.90</td>
</tr>
<tr>
<td>Restaurant and Hotels</td>
<td>0.10</td>
<td>-1.00</td>
<td>-0.90</td>
<td>9.90</td>
</tr>
<tr>
<td>Glass and pottery</td>
<td>-0.10</td>
<td>2.40</td>
<td>2.20</td>
<td>5.40</td>
</tr>
<tr>
<td>Iron and Steel</td>
<td>0.20</td>
<td>7.80</td>
<td>8.00</td>
<td>9.40</td>
</tr>
<tr>
<td>Machinenery</td>
<td>-0.50</td>
<td>27.20</td>
<td>26.40</td>
<td>40.30</td>
</tr>
<tr>
<td>Construction</td>
<td>0.00</td>
<td>2.60</td>
<td>2.60</td>
<td>7.90</td>
</tr>
<tr>
<td>Paper</td>
<td>-0.10</td>
<td>1.80</td>
<td>1.70</td>
<td>5.90</td>
</tr>
<tr>
<td>Other Products</td>
<td>0.10</td>
<td>2.00</td>
<td>2.00</td>
<td>9.30</td>
</tr>
<tr>
<td>Commerce</td>
<td>-0.10</td>
<td>0.70</td>
<td>0.70</td>
<td>3.60</td>
</tr>
<tr>
<td>Transport</td>
<td>0.00</td>
<td>0.90</td>
<td>0.80</td>
<td>3.80</td>
</tr>
<tr>
<td>Real Estate</td>
<td>0.00</td>
<td>1.00</td>
<td>1.00</td>
<td>4.50</td>
</tr>
<tr>
<td>Public Services</td>
<td>0.00</td>
<td>0.00</td>
<td>0.00</td>
<td>0.20</td>
</tr>
<tr>
<td>Financial Services</td>
<td>0.00</td>
<td>1.20</td>
<td>1.20</td>
<td>6.20</td>
</tr>
<tr>
<td>Other Services</td>
<td>0.00</td>
<td>1.70</td>
<td>1.70</td>
<td>5.80</td>
</tr>
<tr>
<td>Total Product</td>
<td>0.10</td>
<td>2.10</td>
<td>2.20</td>
<td>10.40</td>
</tr>
</tbody>
</table>

Source: computed by author from CGE simulations results
and machinery (up 27.2 percent under FTAEU and 26.4 percent under FTAEPA).

The changes in the production of machinery and appliances are quite high in percentage terms, however, production of machinery and appliances in Senegal, currently, is very low, accounting for only 7 percent of total quantity of machines and appliances available, the rest being imported. The high shifts in machinery production, thus, are explained by the fact that production was at a very basic level before the shock. Further, "machinery" includes both machinery and other equipment and appliances; while it is possible that Senegal may produce more appliances under the new environment, an increase of production in machinery at this pace would be less realistic. Therefore, another way to rationalize this increase is to consider the increase in production as mainly coming from the production of appliances; the increase in imports, therefore, is mainly made up of machines.

With the West African Custom Union, the increase in total product is carried mainly by primary goods, with a 0.5 percent increase; manufacturing increases by 0.2 percent on average, while services drop slightly (-0.02 percent). The positive effect in the production of primary goods under this scenario is dominated by fishing, which rises by 3 percent on average, against -0.08 and 0.02 percent shifts for the production of agricultural goods and mining, respectively.

Graphs 2.10-2.12 describe the evolution of the effects of the simulations on skilled and unskilled labor, and total employment. The primary sector (with agriculture and fishing) and services (commerce and public services) are among the main providers of employment in Senegal, therefore the impact on these sectors is of particular importance, at least in the short term. That may explain why employment is negatively affected under the West
African Customs Union scenario (-0.1 percent on average), with a decrease of production in agriculture and commerce. In the production of primary goods, the comparative advantage of Senegal within West Africa resides in fishing. A customs union in the region will increase the exports of fish products (4.8 percent) and the imports of agricultural goods (0.3 percent on average) for Senegal. However, the increase in fishing, in this scenario, is not enough to compensate for the loss of employment mainly due to the decrease of the production of agricultural goods, and commerce. Unskilled labor, the largest share of employment in the economy, shows an adverse effect of twice as much as what is seen skilled labor. Unskilled labor faces negative effects during the first 15 years after the policy change; it starts recovering thereafter, but, the overall effect is negative throughout the simulation period. Skilled labor, on the other hand, shows the same pattern, except that the recovery starts 17 years after the shock; this is not enough to induce an increase in employment overall. Under the West African customs union scenario, the negative effects on employment are smaller compared to those in the others scenarios. Under the FTA with the EU,
Table 5: Average Percentage Shifts in Production from Baseline Values

<table>
<thead>
<tr>
<th></th>
<th>FTAWA</th>
<th>FTAEU</th>
<th>FTAEPA</th>
<th>FTAWORLD</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Production</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Primary goods</td>
<td>0.5</td>
<td>1.1</td>
<td>1.7</td>
<td>9.4</td>
</tr>
<tr>
<td>Manufactured</td>
<td>0.2</td>
<td>3.2</td>
<td>3.3</td>
<td>17.0</td>
</tr>
<tr>
<td>Services</td>
<td>0.0</td>
<td>1.3</td>
<td>1.3</td>
<td>5.4</td>
</tr>
<tr>
<td><strong>Imports</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Manufactured</td>
<td>0.3</td>
<td>3.7</td>
<td>4.0</td>
<td>16.4</td>
</tr>
<tr>
<td>Services</td>
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<td>2.0</td>
<td>2.1</td>
<td>7.3</td>
</tr>
<tr>
<td>Total</td>
<td>0.3</td>
<td>3.4</td>
<td>3.7</td>
<td>17.7</td>
</tr>
<tr>
<td>Primary goods</td>
<td>3.3</td>
<td>7.6</td>
<td>11.3</td>
<td>17.5</td>
</tr>
<tr>
<td><strong>Exports</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Manufactured</td>
<td>4.5</td>
<td>4.5</td>
<td>4.7</td>
<td>20.9</td>
</tr>
<tr>
<td>Services</td>
<td>-0.1</td>
<td>-1.1</td>
<td>-1.2</td>
<td>2.6</td>
</tr>
<tr>
<td>Total</td>
<td>0.3</td>
<td>3.7</td>
<td>4.0</td>
<td>19.8</td>
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<tr>
<td><strong>Absorption</strong></td>
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<td></td>
<td></td>
</tr>
<tr>
<td>Private Consumption</td>
<td>0.1</td>
<td>1.6</td>
<td>1.7</td>
<td>9.4</td>
</tr>
<tr>
<td>Private Investment</td>
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<td>2.5</td>
<td>2.5</td>
<td>7.7</td>
</tr>
<tr>
<td>RGDP</td>
<td>0.1</td>
<td>1.8</td>
<td>1.9</td>
<td>8.9</td>
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<tr>
<td><strong>Income effects</strong></td>
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<td></td>
<td></td>
</tr>
<tr>
<td>Enterprises</td>
<td>0.1</td>
<td>1.8</td>
<td>1.9</td>
<td>10.3</td>
</tr>
<tr>
<td>Households</td>
<td>0.1</td>
<td>1.4</td>
<td>1.5</td>
<td>8.9</td>
</tr>
<tr>
<td>Government</td>
<td>0.2</td>
<td>0.5</td>
<td>0.7</td>
<td>3.9</td>
</tr>
<tr>
<td><strong>Employment</strong></td>
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<tr>
<td>Skilled</td>
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<td>1.0</td>
<td>8.1</td>
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<tr>
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<td>0.1</td>
<td>3.2</td>
</tr>
<tr>
<td>Total</td>
<td>-0.1</td>
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<td>0.2</td>
<td>4.2</td>
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</tbody>
</table>

Source: Computed by author from CGE simulations results.

under the EPA, total employment has overall increased by 0.3 and 0.2 percent on average, respectively; again free trade has the biggest impact, with 4.2 percent increase on total employment. In these three scenarios, skilled labor employment has increased more than unskilled labor, due to the increase in manufacturing and in services (Table 2.4).

Unskilled labor receives a highly adverse effect in the early period of liberalization under free trade, the positive impacts start showing up only more than a decade after implementation. Skilled labor, however, experiences positive effects for all years. Total employment shows a pattern very similar to that of unskilled labor; it experiences negative effects for more than a decade and afterwards, it starts increasing. Therefore, in the early stages of liberalization under free trade, the negative effects on unskilled labor employment outweigh the positive effects on that of skilled labor, leading to an overall decrease in employment. These negative impacts are due to the adverse effects on the commerce, public services and
### Table 6: Average Percentage Shifts on Imports from Baseline Values

<table>
<thead>
<tr>
<th>Category</th>
<th>FTAWA</th>
<th>FTAEU</th>
<th>FTAEPA</th>
<th>FTAWORLD</th>
</tr>
</thead>
<tbody>
<tr>
<td>Agriculture</td>
<td>0.3</td>
<td>2.9</td>
<td>3.2</td>
<td>24.6</td>
</tr>
<tr>
<td>Mining</td>
<td>0.1</td>
<td>3.3</td>
<td>3.4</td>
<td>19.8</td>
</tr>
<tr>
<td>Wood</td>
<td>1.2</td>
<td>2.9</td>
<td>4.1</td>
<td>11.3</td>
</tr>
<tr>
<td>Rubber</td>
<td>0.1</td>
<td>5.4</td>
<td>5.5</td>
<td>20.1</td>
</tr>
<tr>
<td>Fishing</td>
<td>1.9</td>
<td>6.3</td>
<td>8.0</td>
<td>23.1</td>
</tr>
<tr>
<td>Processed food</td>
<td>0.7</td>
<td>2.5</td>
<td>3.2</td>
<td>20.0</td>
</tr>
<tr>
<td>Leather</td>
<td>0.1</td>
<td>9.9</td>
<td>10.1</td>
<td>30.2</td>
</tr>
<tr>
<td>Textile</td>
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<td>5.9</td>
<td>6.8</td>
<td>30.7</td>
</tr>
<tr>
<td>Tobacco</td>
<td>0.1</td>
<td>7.0</td>
<td>7.2</td>
<td>22.6</td>
</tr>
<tr>
<td>Beverages</td>
<td>0.3</td>
<td>13.2</td>
<td>13.5</td>
<td>30.6</td>
</tr>
<tr>
<td>Chemicals</td>
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<td>3.5</td>
<td>3.6</td>
<td>18.5</td>
</tr>
<tr>
<td>Petroleum and Coal</td>
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<td>2.1</td>
<td>2.4</td>
<td>9.3</td>
</tr>
<tr>
<td>Transport equipment</td>
<td>0.0</td>
<td>4.0</td>
<td>4.0</td>
<td>11.1</td>
</tr>
<tr>
<td>Telecommunication</td>
<td>0.0</td>
<td>1.4</td>
<td>1.3</td>
<td>5.5</td>
</tr>
<tr>
<td>Glass and pottery</td>
<td>0.1</td>
<td>6.4</td>
<td>6.4</td>
<td>20.4</td>
</tr>
<tr>
<td>Iron and Steel</td>
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<td>5.6</td>
<td>5.8</td>
<td>13.1</td>
</tr>
<tr>
<td>Machinery</td>
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<td>2.7</td>
<td>10.2</td>
</tr>
<tr>
<td>Paper</td>
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<td>4.5</td>
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</tr>
<tr>
<td>Other Products</td>
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<td>6.8</td>
<td>28.0</td>
</tr>
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<td>Transport</td>
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<td>1.7</td>
<td>1.7</td>
<td>6.6</td>
</tr>
<tr>
<td>Financial Services</td>
<td>0.0</td>
<td>1.8</td>
<td>1.8</td>
<td>8.0</td>
</tr>
<tr>
<td>Other Services</td>
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<td>2.4</td>
<td>8.0</td>
</tr>
<tr>
<td>Total</td>
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<td>3.4</td>
<td>3.7</td>
<td>17.7</td>
</tr>
</tbody>
</table>

Source: Computed by author from CGE simulations results.

### Figure 5: Effects of Different Simulations on Absorption

Source: From Simulation Results
telecommunication activities, which under free trade have decreased in the early years after liberalization.

With the FTAEU, the unskilled labor recovers from the negative shocks 14 years after the shock. Skilled labor, though, is positively affected during the entire period, but these effects are not enough to compensate for the loss in unskilled labor employment in the first decade, explaining the low effects on employment overall.

The effects of the EPA are shaped by the influences of the West African customs union and the FTA with the EU. In this scenario, skilled labor employment is positively affected throughout the entire period of simulation. Unskilled labor, on the other hand, decreases in the first decade, but recovers in the second decade after the shock. The negative effects in this scenario come from the decrease, in the first years of the policy changes, in production in sectors such as agriculture, commerce, and public services.

The effects of FTAWA on real GDP are small, with an increase of 0.1 percent on average compared to those under FTA EU and FTA EPA, under which the effects are of a higher
Table 7: Average Percentage Shifts on Exports from Baseline Values

<table>
<thead>
<tr>
<th></th>
<th>FTAWA</th>
<th>FTAEU</th>
<th>FTA EPA</th>
<th>FTAWORLD</th>
</tr>
</thead>
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<td>Agriculture</td>
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<td>-2.1</td>
<td>-0.3</td>
<td>18.6</td>
</tr>
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<td>Mining</td>
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<td>0.0</td>
<td>1.2</td>
</tr>
<tr>
<td>Wood</td>
<td>2.0</td>
<td>-2.7</td>
<td>2.0</td>
<td>2.4</td>
</tr>
<tr>
<td>Rubber</td>
<td>0.1</td>
<td>3.9</td>
<td>0.0</td>
<td>19.1</td>
</tr>
<tr>
<td>Fishing</td>
<td>4.8</td>
<td>6.0</td>
<td>4.9</td>
<td>5.8</td>
</tr>
<tr>
<td>Processed food</td>
<td>0.6</td>
<td>-1.2</td>
<td>0.5</td>
<td>19.2</td>
</tr>
<tr>
<td>Leather</td>
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<td>-0.9</td>
<td>13.6</td>
</tr>
<tr>
<td>Textile</td>
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<td>0.0</td>
<td>0.3</td>
<td>6.7</td>
</tr>
<tr>
<td>Tobacco</td>
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<td>1.0</td>
<td>-0.2</td>
<td>11.3</td>
</tr>
<tr>
<td>Beverages</td>
<td>4.0</td>
<td>0.0</td>
<td>10.0</td>
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<td>Chemicals</td>
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<td>3.1</td>
<td>0.1</td>
<td>13.6</td>
</tr>
<tr>
<td>Petroleum and coal</td>
<td>0.2</td>
<td>3.7</td>
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<td>14.8</td>
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<tr>
<td>Transport equipment</td>
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<td>-0.5</td>
<td>11.3</td>
</tr>
<tr>
<td>Telecommunication</td>
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<td>-0.5</td>
<td>-1.9</td>
</tr>
<tr>
<td>Restaurant and hotels</td>
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<td>-2.3</td>
<td>0.1</td>
<td>12.4</td>
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<tr>
<td>Glass and pottery</td>
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<td>4.3</td>
</tr>
<tr>
<td>Iron and Steel</td>
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<td>0.3</td>
<td>1.6</td>
</tr>
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<td>Machinery</td>
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<td>-0.2</td>
<td>5.9</td>
</tr>
<tr>
<td>Other Products</td>
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<td>3.3</td>
<td>0.1</td>
<td>11.4</td>
</tr>
<tr>
<td>Transport</td>
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<td>-0.2</td>
<td>-0.9</td>
</tr>
<tr>
<td>Financial Services</td>
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<td>-0.4</td>
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<tr>
<td>Other Services</td>
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<td>-0.2</td>
<td>0.5</td>
</tr>
<tr>
<td>Total</td>
<td>0.3</td>
<td>3.7</td>
<td>4.0</td>
<td>19.8</td>
</tr>
</tbody>
</table>

Source: Computed by author from CGE simulations results.
magnitude, with an increase of 1.8 and 1.9 percent on average, respectively. Private consumption and investment also increase, with again the FTAWA causing the smallest impact and the free trade scenario, the largest.

Imports and exports increase in all scenarios, therefore, trade overall has increased. As a result, discussing the issue of trade diversion becomes less relevant; for, the acceptance of an FTA by the WTO relies on the condition that it increases trade overall. In general, the effects of FTAWA on Senegal’s economy are small compared to those of FTAEU and FTAEPA; consequently, the effects of the EPA closely mirror those of FTAEU.

Four major points stand out among the results analyzed above. First, the condition of EU that the WA countries set up a customs union before the EPA is of less relevance in the case of Senegal, and by extension for WA countries in general. Second, employment, of unskilled labor in particular, will be negatively affected in a period extending for more than a decade. Employment during the first decade of the EPA has decreased by 0.2 percent on average due to the loss of employment of unskilled labor. The positive effects in
the second decade, however, outweigh the negative effects in the first, leading to a positive impact overall. Therefore, in facilitating the transition, programs should focus on educating and training unskilled workers, bearing in mind that the transition will take at least a decade. Third, agriculture is the most affected sector, with negative impacts over the entire period covered. It would, therefore, be necessary to help farmers focus their efforts on the production of a few crops in which Senegal could be efficient given the new environment, and help the inefficient farmers convert to alternative activities such as livestock, fishing, among others. Finally, for the fourth point, it appears that free trade represents the best option, even though the short-term cost, in terms of unemployment, is larger compared to other scenarios, during the first decade after the shock.

5.3 Sensitivity Analysis

The results of CGE models are often said to depend greatly on the magnitudes of some parameters (elasticities) and on the closure of the model. I conducted a sensitivity analysis
The Armington elasticities are at the center of most of the criticisms against CGE models. Larger elasticities imply a high degree of substitutability between domestic and foreign varieties of a good. Ruhl (2008) argues that economic actors have different reactions when they experience temporary or permanent changes. Permanent changes often induce bigger adjustments compared to temporary ones. Tariff removal or decrease, being permanent, thus, tends to be related to an increase in the size of elasticities. He found that a tariff change increases the elasticity to 6.4 compared to 1.2 with temporary changes. On this basis, I inflated the elasticities in Table 3 by 5, taking them from an average of 1.1 to 6.1.

The second issue for the robustness check addresses the closure of the model. The main results are based on a flexible exchange rate, and sales tax rates, which allows for fixed foreign saving and government expenditure. I relax these two assumptions, by adopting a fixed exchange rate and tax rates, which allows for flexible foreign and government savings.

The effects of the EPA on real GDP, employment, and total imports, in these two
Figure 14: Effects of the EPA on Real GDP Using Different Elasticities and a Different Closure

alternatives, are presented in Graphs 2.15-2.18, along with the effects of the EPA in the main results. This analysis shows that, while the magnitude of some impacts change with different elasticities and closure, the directions of the impacts remain the same. The effects on real GDP are robust to the change in elasticities. The closure, however, gives lower effects compared to the original closure. Employment receives higher adverse effects when different elasticities and closure are used, with the recovery starting later compared to the main results. Finally, the effects on imports are higher when different elasticities are used and lower with the alternative closure. As mentioned therefore, the directions of the effects, under the different alternatives follow the same patterns as those in the main results. Thus, the analysis, in terms of policy implications, stay the same.
6 Conclusion

This paper analyzed the consequences on Senegal’s economy of an economic partnership agreement (EPA) between the EU and West African countries (WA), using a recursive dynamic general equilibrium. The results found in this paper indicate that sectors such as agriculture, very intensive in unskilled labor, receive some adverse effects for more than a decade; consequently, unskilled labor employment is negatively affected in the transition period. The results also show that, in the case of Senegal, integrating a WA customs union into the EPA does not make much difference. That is probably what explains the difficulties in reaching an agreement on the customs union currently. The EPA affects real GDP positively, which probably comes from Senegal developing its manufacturing sector. The results found are checked for robustness, and the patterns are not affected much, which leaves the recommendations based on the main results still relevant.

Further, on May 2010, the EU responded favorably to the WA countries’ request of a fund "to reap the benefit and mitigate the negative effects of the EPA" (Trade Negotiation Insight). The EPA development program (EPADP) funds will be aimed at issues such as the diversification and production capacities, the development of intra-regional trade and facilitation of access to international markets, and improvement and reinforcement of trade-related facilities. These funds, therefore, could be used to help workers adjust to the new environment, by helping them reconvert to new jobs, and improve the capacity of exporters, by building trade related infrastructure, which will make the regional market in WA more accessible for the development of the manufacturing sectors.
References


A. The equations of the model

A.1 Static Model

A.1.1 Price Bloc

\[ P_{m_c} = P_{wm_c} (1 + t_{mc}) \cdot EXR + \sum_{c'} P_{q_{c', icm_c'}} \]  
(7)

\[ P_{e_c} = P_{we_c} \cdot EXR + \sum_{c'} P_{q_{c', ice_c'}} \]  
(8)

\[ P_{mr_c} = P_{wmr_{cr}} (1 + t_{mr_c}) \cdot EXR + \sum_{c'} P_{q_{c', icm_{c'}}} \]  
(9)

\[ P_{er_c} = P_{wer_{cr}} \cdot EXR + \sum_{c'} P_{q_{c', ice_{c'}}} \]  
(10)

\[ P_{dd_c} = P_{ds_c} + \sum_{c'} P_{q_{c', icd_{c'}}} \]  
(11)

\[ P_{q_c} (1 - t_{q_c}) Q_{c} = P_{dd_c} Q_{d_c} + P_{m_c} Q_{m_c} \]  
(12)

\[ P_{x_c} Q_{x_c} = P_{ds_c} Q_{d_c} + P_{e_c} Q_{e_c} \]  
(13)

\[ (1 - t_{a}) P_{a} Q_{a} = P_{int} Q_{int} + P_{v_a} Q_{v_a} \]  
(14)

\[ P_{int_a} = \sum_{c} P_{q_{c, ica_{ca}}} \]  
(15)

\[ CPI = \sum_{c'} P_{q_{c, cwts_c}} \]  
(16)

\[ DPI = \sum_{c'} P_{ds_c, dwts_c} \]  
(17)

A.1.2 Households

Households maximize their utilities under their the constrain that total expenditure equals total income. The solutions gives the demand and expenditure functions for each commodity in equations 7 and 8 respectively.

\[ Q_{c} = \gamma_{c} + \frac{\beta_{c}^m}{P_{q_c}} \left( EH - \sum P_{q_{c, \gamma_{c, m}}^{c}} \right) \]  
(18)

\[ P_{q_c} Q_{c} = P_{q_{c, \gamma_{c}} + \beta_{c}^{m}} \left( EH - \sum P_{q_{c, \gamma_{c}^{m}}} \right) \]  
(19)

\[ EH = \left( 1 - \sum s_{h_{ih}} \right) (1 - mps_{h}) (1 - tins_{h}) Y_{h} \]  
(20)
A.1.3 Production Bloc

Goods and services are produced by firms that maximize profit in a perfect competition framework. Each activity produces one good and combines VA and intermediates in a fixed proportion for a given quantity of production.

\[ Q_{va} = iv_{a}Q_{a} \]
\[ Q_{inta} = int_{a}Q_{a} \quad (21) \]
\[ Q_{inta} = ica_{ac}Q_{inta} \quad (22) \]
\[(1 - t_{a})P_{a}Q_{a} = P_{va}Q_{va} - P_{inta}Q_{inta} \quad (23) \]
\[ Q_{va} = \alpha v_{a} \left( \sum_{f} \delta_{v_{fa}} \left( \alpha v_{fa} Q_{f_{fa} - \rho_{va}} \right) \right)^{-1} \quad (24) \]
\[ W_{f_{fa}} = (1 - tv_{a})P_{va}Q_{va} \left( \sum_{f} \delta_{v_{fa}} \left( \alpha v_{fa} Q_{f_{fa} - \rho_{va}} \right) \right)^{-1} \delta_{v_{fa}} \left( \alpha v_{fa} Q_{f_{fa} - \rho_{va}} \right)^{-1} \quad (25) \]

A.1.4 Output Transformation

Domestically produced outputs are either sold domestically or exported. Producers maximize their revenues \( (TR) \) on both markets subject to a constant elasticity of transformation and prices. imperfect substitutability

\[ TR = P_{xc}Q_{xc} \quad (26) \]
\[ Q_{xc} = \alpha t_{c} \left( \delta t_{c} Q_{e_{c}^{\rho_{tc}}} + (1 - \delta t_{c}) Q_{d_{c}^{\rho_{tc}}} \right)^{\frac{1}{\rho_{tc}}} \quad (27) \]
\[ P_{xc}Q_{xc} = P_{e_{c}}Q_{e_{c}} + P_{d_{c}}Q_{d_{c}} \quad (28) \]
\[ \frac{Q_{d_{c}}}{Q_{e_{c}}} = \frac{1 - \delta t_{c}}{\delta t_{c}} \left( \frac{P_{e_{c}}}{P_{d_{c}}} \right)^{\frac{1}{\rho_{tc} - 1}} \quad (29) \]
\[ \rho_{tc} \geq 1 \implies \text{isoquant concave to the origin} \quad (30) \]
\[ Q_{xc} = Q_{e_{c}} + Q_{d_{c}} \quad (31) \]

imperfect substitutability between output sold on domestic markets and exported. A change in \( \frac{P_{d_{c}}}{Q_{e_{c}}} \) shift supply toward the destination offering a higher price. When one the
markets is not supplied then

A.1.5 Composite Supply

Composite supply is made of goods produced domestically and imported, combined in a CES function, which captures the imperfect substitutability between goods from the 2 origins. Armington function

\[
Q_c = \alpha c \left( \delta c_r Q_{m_r}^{-\rho c} + (1 - \delta c_r) Q_{d_r}^{-\rho c} \right)^{-\frac{1}{\rho c}} \quad (32)
\]

\[
\frac{Q_m}{Q_d} = \frac{1 - \delta c_r}{\delta c_r} \left( \frac{P_{d_c}}{P_{m_c}} \right)^{\frac{1}{\rho c + 1}} \quad (33)
\]

\[
\rho c \geq -1 \quad (34)
\]

\[
Q_c = Q_{d_c} + Q_{m_c} \quad (35)
\]

An increase in \( \frac{P_{d_c}}{P_{m_c}} \), shifts supply toward foreign goods. For goods not produced domestically or not imported, the Armington function is replaced by

A.1.6 International Trade

Regional Exports to different regions are aggregated in a CES function, allowing imperfect substitution between different destinations.

\[
Q_{e_r} = \alpha e_r \left( \sum_r \delta_{e_r, r} Q_{e_r}^{-\rho e_r} \right)^{-\frac{1}{\rho e_r}} \quad (36)
\]

\[
\frac{P_{e_{r_c}}}{P_{e_c}} = Q_{e_r} \left( \sum_r \delta_{e_r, r} Q_{e_r}^{-\rho e_r} \right)^{-1} \delta_{e, r, c} Q_{e_r}^{-\rho e_r - 1} \quad (37)
\]

Regional Imports from different regions are aggregated in a CES function, allowing imperfect substitution between different origins.
\[ Qm_c = \alpha m_c \left( \sum_r \delta m_{rc}.Q_{mr_{rc}}^\rho_c \right)^{-\frac{1}{\rho m_c}} \]  
\[ \frac{P_{mr_{rc}}}{Pm_c} = Qm_c \left( \sum_r \delta m_{rc}.Q_{mr_{rc}}^\rho_c \right)^{-1} \delta m_{rc}.Q_{mr_{rc}}^{-\rho m_c}^{-1} \] 

(38)  
(39) 

Factor Income

\[ Y_{ff} = \sum_a W_{ff.dfa}Q_{ffa} \]  
\[ Y_{if_{if}} = sh_{if_{if}}(Y_{ff} - trsf_{wf}.EXR) \]  
\[ Y_{ii} = \sum_f Y_{if_{if}} + \sum_i Tri_{ig} + trsf_{ig}.CPI + trsf_{iw}.EXR \]  
\[ Tri_{ii} = sh_{if_{if}}.(1 - mps_i). (1 - tins_i). Y_{ih} \] 

(40)  
(41)  
(42)  
(43) 

A.1.7 Government

\[ Yg = \sum_i tins_i.Y_{ii} + \sum_a t_a.P_a.Q_a + \sum_c tm_c.pwm_c.Qm_c.EXR + \sum_c tm_c.pwm_c.Qm_c.EXR \]  
\[ + \sum_r \sum_c tmr_{cr}.pwmr_{cr}.Qmr_{cr}.EXR + \sum_c tq_c.Pq_c.Qc_c + \sum_a Y_{gf} + trsf_{gw}.EXR \] 

(44) 

\[ EG = \sum_c Pq_c.Q_{gc} + \sum_i trsf_{igov}.CPI \] 
\[ Q_{gc} = qadj.Q_{gc} \] 
\[ Q_{inv_c} = iadj.Q_{inv_c} \] 

(45)  
(46)  
(47)
A.1.8 Constraints and Macro-closures

\[ Q_{cc} = \sum_a Q_{int,ca} + \sum_h Q_{h,ch} + Q_{g,c} + Q_{inv,c} + qdist_c + Q_{t,c} \]  
\[ \sum_a Q_{f,fa} = Q_{fs,f} \]  
\[ Y_{g} = E_{g} + G_{sav} \]

\[ \sum_c \sum_r \sum_f \text{pwm}_c \cdot Q_{m,c} + \sum_r \sum_f \text{pwm}_{cr} \cdot Q_{m,cr} + \sum_f \text{trsf}_{wf} = \sum_c \sum_r \sum_f \text{pwe}_c \cdot Q_{e,c} + \sum_r \sum_f \text{pwe}_{cr} \cdot Q_{er,cr} \]  
\[ + \sum_i \text{trsf}_{iw} + F_{sav} \]  
\[ \sum_i \text{mps}_i \cdot (1 - \text{tins}_i) \cdot Y_{i} + G_{sav} + F_{sav} \cdot EXR = \sum_c P_{q,c} \cdot Q_{inv} + \sum_c P_{q,c} \cdot qdist_c \]  
\[ \text{mps}_i = \frac{\text{mps}_i \cdot (1 + \text{mpsadj})}{100} \]

A.1.9 Capital Accumulation

\[ Aw_{f,ft} = \sum_a \left[ \left( \frac{Q_{f,fa,t}}{\sum Q_{f,fa}} \right) \cdot W_{f,ft} \cdot W_{dist,a,ft} \right] \]  
\[ \eta_{fat} = \left( \frac{Q_{f,fa,t}}{\sum Q_{f,fa}} \right) \left[ \beta^a \left( \frac{W_{f,ft} \cdot W_{dist,fa}}{Aw_{f,fa}^a} - 1 \right) + 1 \right] \]  
\[ \nabla K_{fat}^a = \eta_{fat}^a \cdot \frac{\sum_c P_{q,ct} \cdot Q_{inv,ct}}{P_{k,ft}} \]  
\[ P_{k,ft} = \sum_c P_{q,ct} \cdot \frac{Q_{inv,ct}}{\sum Q_{inv,ct}} \]

\[ Q_{f,fa,t+1} = Q_{f,fa,t} \left( 1 + \frac{\nabla K_{fat}^a}{Q_{f,fa,t} - v_{f}} \right) \]  
\[ Q_{f,fs,t+1} = Q_{f,fs,t} \left( 1 + \frac{\nabla K_{fat}^a}{Q_{f,fs,t} - v_{f}} \right) \]
Endogenous Variables

$P_{qc}$ Price of Composite commodity c
$P_a$ The activity price, that is the gross revenue per unit of activity.
$P_{inta_a}$ Aggregate intermediate input price for activity a
$P_{xc}$ Aggregate producer price for commodity
$W_{f_f}$ Average price of factor f
$P_{va}$ Value-added price (factor income per unit of activity)
$P_{mc}$ Import price (domestic currency)
$P_{ec}$ Export price (domestic currency)
$P_{mr_c}$ Import price by region (domestic currency)
$EXR$ Exchange rate (LCU per unit of FCU)
$P_{qc}$ Composite commodity price
$Pe$ Export price by region (domestic currency)
$P_{dc}$ Demand price for commodity produced and sold domestically
$P_{ds_c}$ Supply price for commodity produced and sold domestically
$DPI$ Producer price index
$Awf_{ft}$ Average capital rental rate in time period t
$W_{fk}$ Average price of factor
$Pk_{ft}$ Unit price of capital in time period t
$Q_{c}$ Quantity of commodity c consumed by households
$Q_{f a_t}$ Quantity demanded of factor f from activity a in time period t
$EH$ Consumption spending of households
$Q_a$ The level of output by activity A, it corresponds to the domestic production
$Q_{inta_a}$ Quantity of commodity c as intermediate to activity a
$Q_{f_f}$ Quantity of factor f
$Q_{inta_a}$ Quantity of aggregate intermediate input
$Q_{xc}$ Aggregated quantity of domestic output of commodity
$Q_{c}$ Quantity of goods supplied to domestic market (composite supply)
$Q_{mc}$ Quantity of imports of commodity c
$Q_{dc}$ Quantity sold domestically of domestic output
$Q_{e}$ Quantity of exports
$Q_{va}$ Quantity of (aggregate) valueadded
$Q_{fa_t}$ Quantity demanded of factor f from activity a
$Q_{g_c}$ Government consumption demand for commodity
$Q_{inv_c}$ Quantity of investment demand for commodity
$Q_{hc_c h}$ Quantity consumed of commodity c by household h
$qdst_c$ Quantity of stock change
$Y_f$ Income of factor f
$Y_{if i f}$ Income to domestic institution i from factor f
$Tri_{i i}$ Transfers from institution i’ to i
$Y_{if i f}$ Transfer from factor f to institution i
$shi_{i_f}$ Share for domestic institution i in income of factor f
$Y_{i}$ Income of domestic non-government institution
$mps_{i}$ Marginal propensity to save for domestic non-government institution (exogenous variable)
$Y_{g}$ Government revenue
$EG$ Government expenditures
**Parameters**

- $t_a$: Tax rate for activity $a$
- $t_{mr_c}$: Import price by region (foreign currency)
- $t_q$: Rate of sales tax
- $t_{mc}$: Import price (foreign currency)
- $d_{fa}$: Wage distortion factor for factor $f$ in activity $a$
- $ic_{a,c}$: Quantity of commodity $c$ per unit of aggregate intermediate input
- $it_a$: Quantity of value added per unit of activity
- $il_a$: Quantity of aggregate intermediate input per unit of activity
- $icm_{c,c'}$: Quantity of commodity $c$ as trade input per imported unit of $c'$
- $ic_{c,c'}$: Quantity of commodity $c$ as trade input per exported unit of $c'$
- $icd_{c,c'}$: Quantity of commodity $c$ as trade input per unit of $c'$ produced and sold domestically
- $ic_{c,a}$: Quantity of $c$ as intermediate input per unit of activity $a$
- $cwts_c$: Weight of commodity $c$ in the CPI
- $dwts_c$: Weight of commodity $c$ in the DPI
- $\gamma_{c'}$: Subsistence consumption of marketed commodity $c$ for household
- $\beta_c$: Marginal share of consumption spending on marketed commodity $c$ for household
- $\eta_{f,a,t}^i$: The share of new capital for each sector
- $\alpha^u_a$: Efficiency parameter in the CES value added function
- $\delta_{fa}$: CES value-added function share parameter for factor $f$ in activity $a$
- $\rho_{fa}$: CES value-added function exponent
- $\alpha_{c,a}$: CET function shift parameter
- $\delta_{c,a}$: CET function share parameter
- $\rho_{c,a}$: CET function exponent
- $\alpha_{c,c}$: Armington function shift parameter
- $\rho_{c,c}$: Armington function exponent
- $\delta_{c,c}$: Armington function share parameter
- $\alpha_{c,c}$: Shift parameter in the CES regional export function
- $\delta_{e_{r,c}}$: Share parameter in the CES regional export function
- $\rho_{e_{r,c}}$: Regional exports aggregation function exponent
- $\alpha_{m,c}$: Shift parameter in the CES regional import function
- $\delta_{m,c}$: Share parameter in the CES regional import function
- $\rho_{m,c}$: Regional imports aggregation function exponent
- $\nu_f$: Capital depreciation rate
- $\overline{mps}_i$: Base savings rate for domestic institution $i$
- $Rwf_{f}$: Real average factor price
- $P_{wm_c}$: Import price (foreign currency)
- $P_{wmr_{cr}}$: Import price by region (foreign currency)
- $P_{we_{r,c}}$: Export price by region (foreign currency)
- $P_{we_c}$: Export price (foreign currency)
- $Q_{g_c}$: Base-year quantity of government demand
- $Q_{inv_c}$: Base-year quantity of private investment demand
- $\overline{tins}_i$: Exogenous direct tax rate for domestic institution $i$

**Exogenous variables**

- $mpsadj_f$: Savings rate scaling factor
- $Wf_{distf_{at}}$: Wage distortion factor for factor $f$ in activity $a$
- $Qfs_f$: Quantity Supplied of factor
- $CPI$: Consumer price index
- $gadj$: Government consumption adjustment factor
- $iadj$: Investment adjustment factor
- $Fsav$: Foreign savings (FCU)
- $Gsav$: Government savings