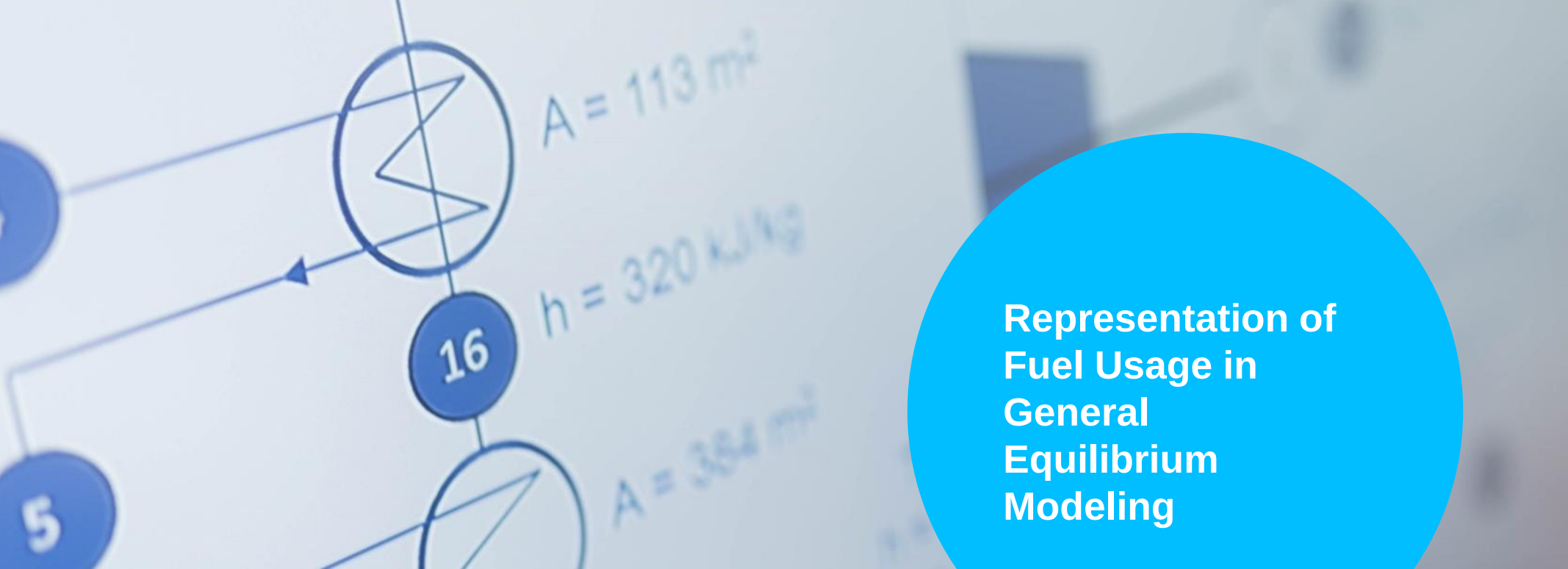




## Representation of Fuel Usage in General Equilibrium Modeling

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# Introduction

„Recently, I found an interesting behavior in our model...”



Mi 14.12.2022 16:21

Siegle, Jonathan

gas and oil usage in EPPA

An chenyh@mit.edu

Dear Dr Chen,

My name is Jonathan Siegle and I am a research assistant working with the CGE model NEWAGE at the University of Stuttgart, Germany. The NEWAGE model is written in GAMS/MPGSE and the main data source is GTAP 10, so there are quite some similarities to EPPA.

Recently, I found an interesting behavior in our model, and it might be present in the EPPA model as well:

Under carbon pricing, the use of gas declines faster than the use of oil.

This is counterintuitive, because the emission factor of gas is lower than that of oil.

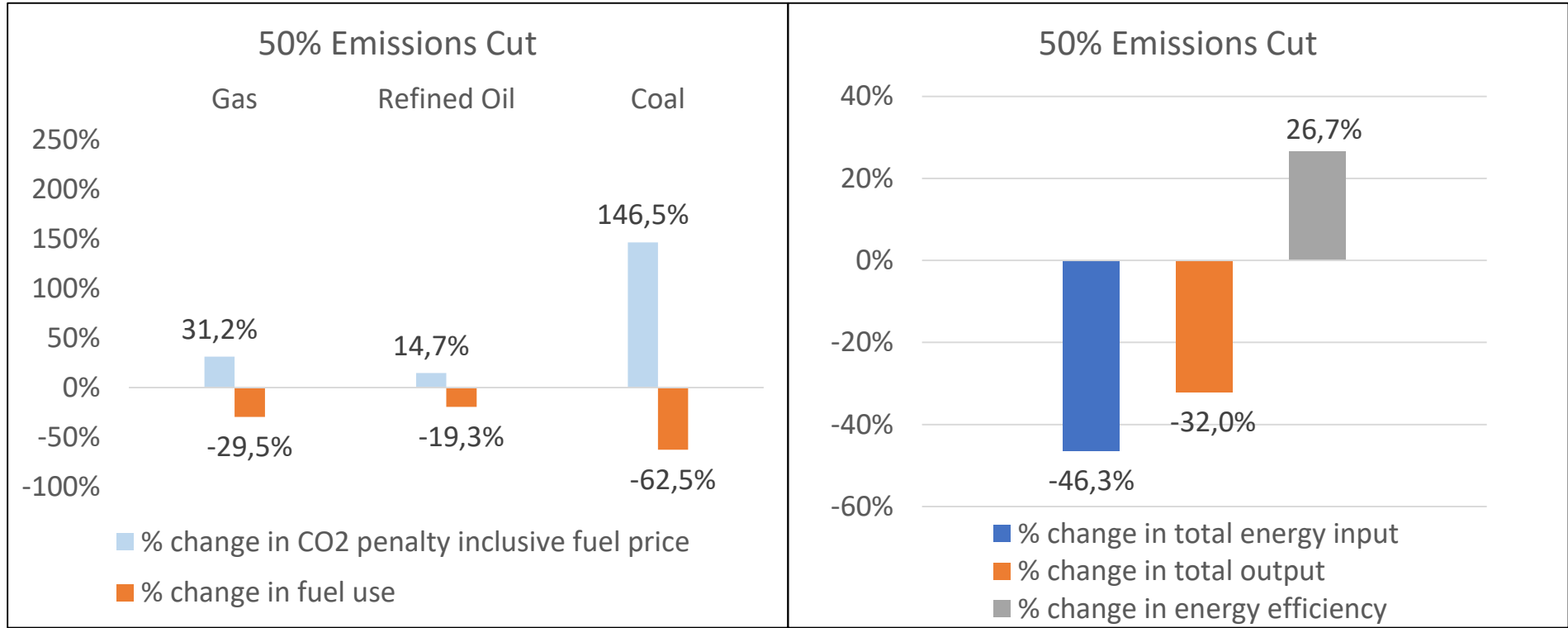
## Simple Outline: SAM of the 1-2-4 model (Markusen, 2006)

|         | Production sectors |     |      | Consumers |
|---------|--------------------|-----|------|-----------|
| Markets | X                  | Y   | W    | CONS      |
| PX      | 100                |     | -100 |           |
| PY      |                    | 100 | -100 |           |
| PW      |                    |     | 200  | -200      |
| PG      | -25                | -25 |      | 50        |
| PO      | -25                | -25 |      | 50        |
| PA      | -25                | -25 |      | 50        |
| PK      | -25                | -25 |      | 50        |

## Simple Outline: Input Structure of Sector X

|     |                                             | Source    | G     | O     | A     | K  |
|-----|---------------------------------------------|-----------|-------|-------|-------|----|
| [1] | Capital input (bn \$)                       | assumed   |       |       |       | 25 |
| [2] | Energy input (bn \$)                        | assumed   | 25    | 25    | 25    |    |
| [3] | Energy input (EJ)                           | = [2]/[4] | 6.08  | 2.60  | 10.69 |    |
| [4] | Energy price (bn \$/EJ)                     | GTAP11    | 4.1   | 9.6   | 2.3   |    |
| [5] | Emissions per EJ (Mt-CO <sub>2</sub> /EJ )  | EPPA      | 50.23 | 72.97 | 90.53 |    |
| [6] | Emissions (Mt-CO <sub>2</sub> )             | = [3]*[5] | 305.2 | 189.7 | 968.2 |    |
| [7] | Emissions /bn\$ (Mt-CO <sub>2</sub> /bn \$) | = [6]/[2] | 12.2  | 7.6   | 38.7  |    |

## Simple Outline: Value-Related Emissions Factor determines Fuel Use under Carbon Pricing



# Problem Statement

## Problem Statement

### 1. The Substitution Pattern

Consider two fossil fuels.

A fossil fuel with a lower energy-related emissions coefficient can have a higher value-related emissions coefficient – if its energy price is lower.

Under carbon pricing, it therefore incurs a higher penalty. Consequently, its usage in a production function declines more.

### 2. Energy Efficiency Changes

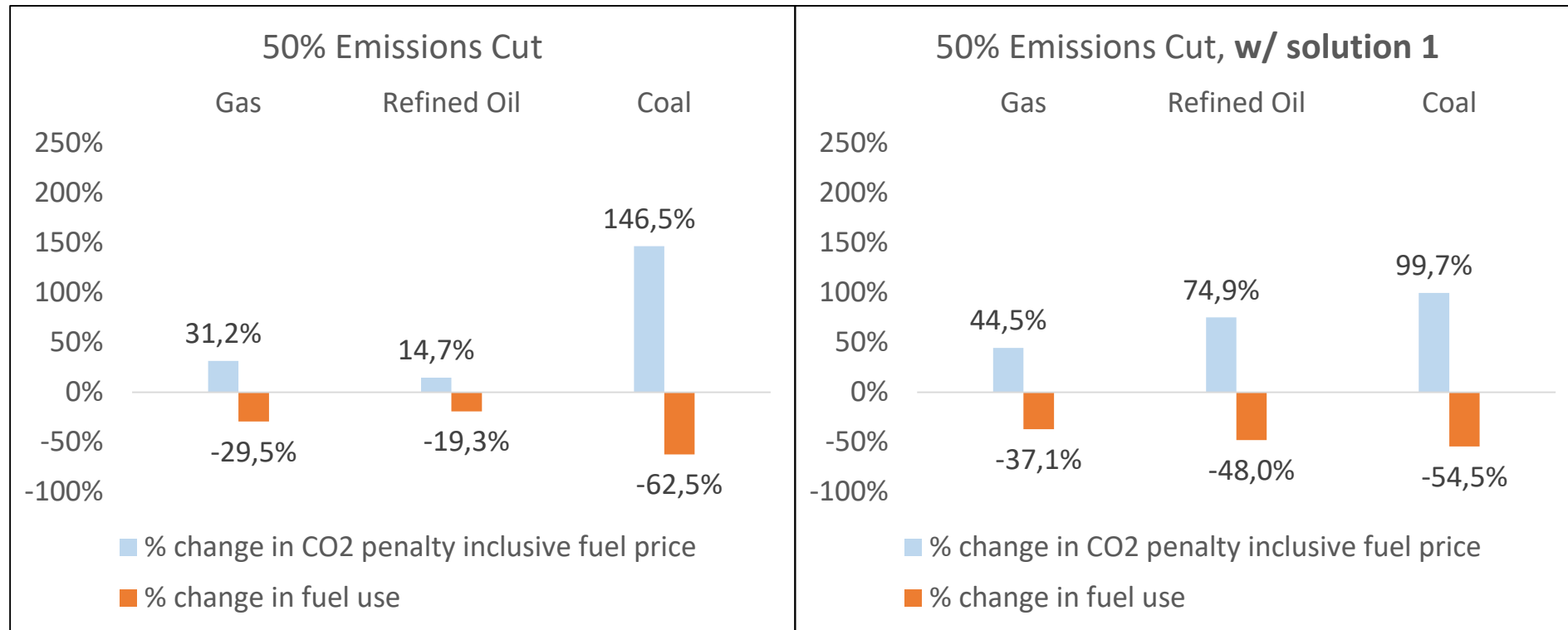
Inter-fuel substitution in a production function can inadvertently change energy use levels in physical units. Energy efficiency of production is therefore more likely to get improved beyond physically realistic measures.

**Solution 1:  
Fuel Substitution Based  
on Physical Quantities**

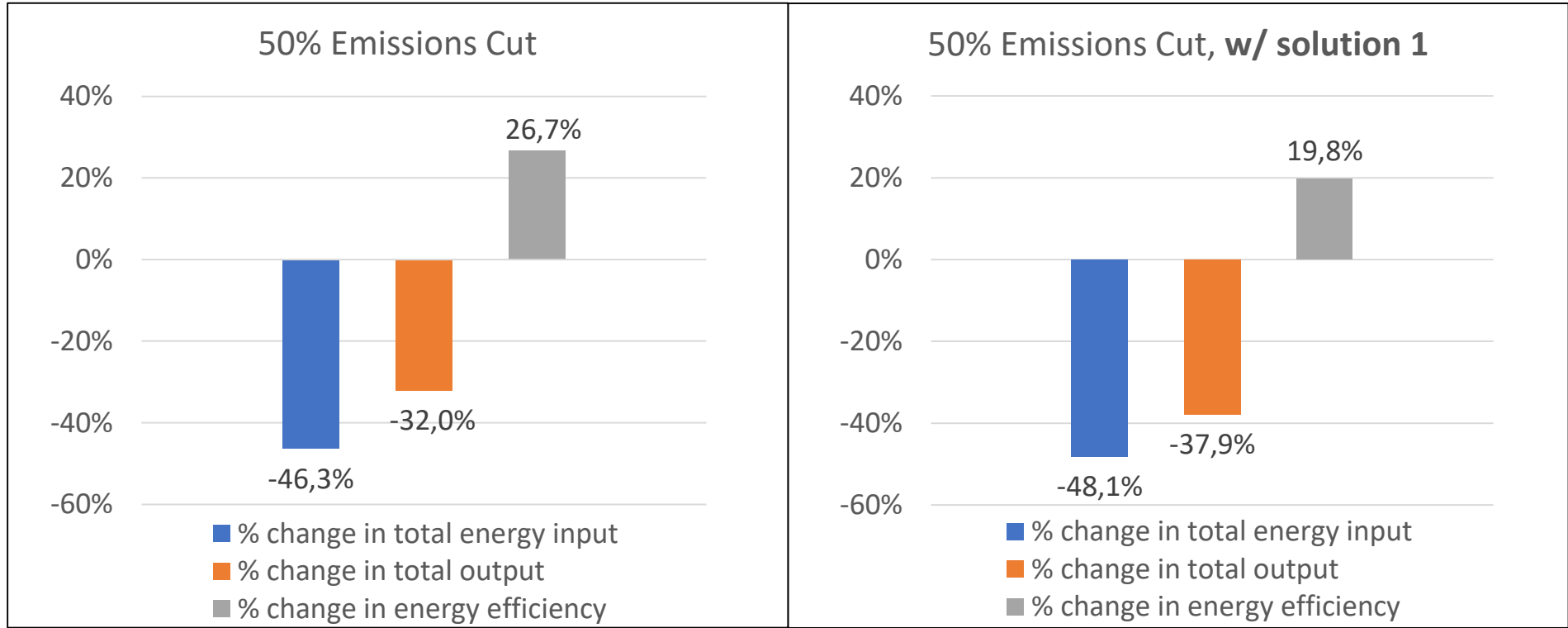
## Solution 1: Fuel Substitution Based on Physical Quantities

| Measure                                                                                                                                                                                                                                                                                                                             | Rationale                                                                                                                                                                                      |
|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <b>Eliminate the base year fuel price differences:</b><br>Value all physical fossil fuel reference quantities with the same price                                                                                                                                                                                                   | → A “dollar-to-dollar” fuel substitution is now also a “joule-to-joule” exchange<br>→ under carbon pricing, the structure of emissions per dollar is consistent to that of emissions per joule |
| <b>Impose taxes or subsidies on fuel consumption</b>                                                                                                                                                                                                                                                                                | → In the base year, the after-tax consumer price of each fuel remains the same as the pre-adjusted level                                                                                       |
| <b>Impose taxes or subsidies on fuel production</b><br>For each fuel: If the pre-adjusted price is...<br>...higher than the price used for valuation, use the tax revenue to subsidize the fuel’s own production.<br>...lower than the price used for valuation, raise the subsidy payment from a tax on the fuel’s own production. | → The corresponding zero-profit conditions are retained                                                                                                                                        |

## Solution 1: Both Issues Resolved...



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## Solution 1: Both Issues Resolved...

### 1. The Substitution Pattern



Consider two fossil fuels.

A fossil fuel with a lower energy-related emissions coefficient can have a higher value-related emissions coefficient – if its energy price is higher.

Under carbon pricing, it therefore incurs a higher penalty. Consequently, its usage in a production function declines more.

### 2. Energy Efficiency Changes



Inter-fuel substitution in a production function can inadvertently change energy use levels in physical units.

Energy efficiency of production is therefore more likely to get improved beyond physically realistic measures.



## Solution 1: Discussion

### 1. The Substitution Pattern

Should this really get „resolved“?

- (Paltsev et al. 2005): Just as land prices assign different values to the size of different parcels, energy prices assign different values to the energy content of different energy carriers.
- (Cleveland et al. 2000): There are other factors besides energy content that lead to differentiated valuation of fuels.

## Solution 1: Discussion

### 1. The Substitution Pattern

Does carbon pricing increase the relative importance of energy content among other value-determining attributes of fuels  
?

Carbon pricing  
↓  
scarcity of energy carriers  
↓  
“core attribute” energy content increasingly important  
↓  
economic value getting aligned with energy content  
?

**Solution 2:  
Energy Efficiency  
Constraint**

## Solution 2: Energy Efficiency Constraint

Energy Efficiency Index:

$$\gamma = \frac{X / (gxp \cdot GX + oxp \cdot OX + axp \cdot AX)}{1 / (gxp + oxp + axp)}$$

- $X$  is the output index for sector  $X$
- $GX$ ,  $OX$ , and  $AX$  are the consumption indices of G, O, and A fuel inputs to  $X$
- $gxp$ ,  $oxp$ , and  $axp$  are the energy contents of  $GX$ ,  $OX$  and  $AX$  in physical units

## Solution 2: Energy Efficiency Constraint

Energy Efficiency Index:

$$\gamma = \frac{X / (gxp \cdot GX + oxp \cdot OX + axp \cdot AX)}{1 / (gxp + oxp + axp)} \leq 1.1$$

- $X$  is the output index for sector  $X$
- $GX$ ,  $OX$ , and  $AX$  are the consumption indices of G, O, and A fuel inputs to  $X$
- $gxp$ ,  $oxp$ , and  $axp$  are the energy contents of  $GX$ ,  $OX$  and  $AX$  in physical units

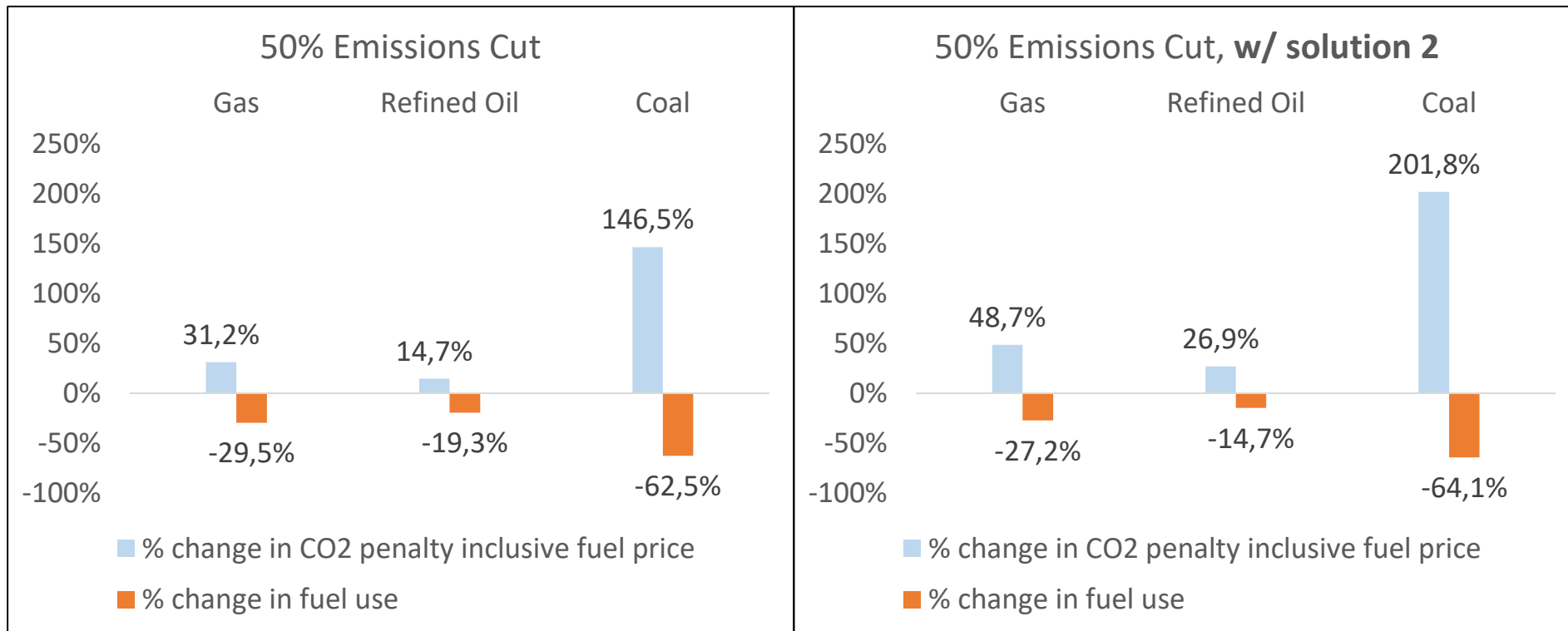
## Solution 2: Energy Efficiency Constraint: Enable Adherence

Output tax & input subsidy:

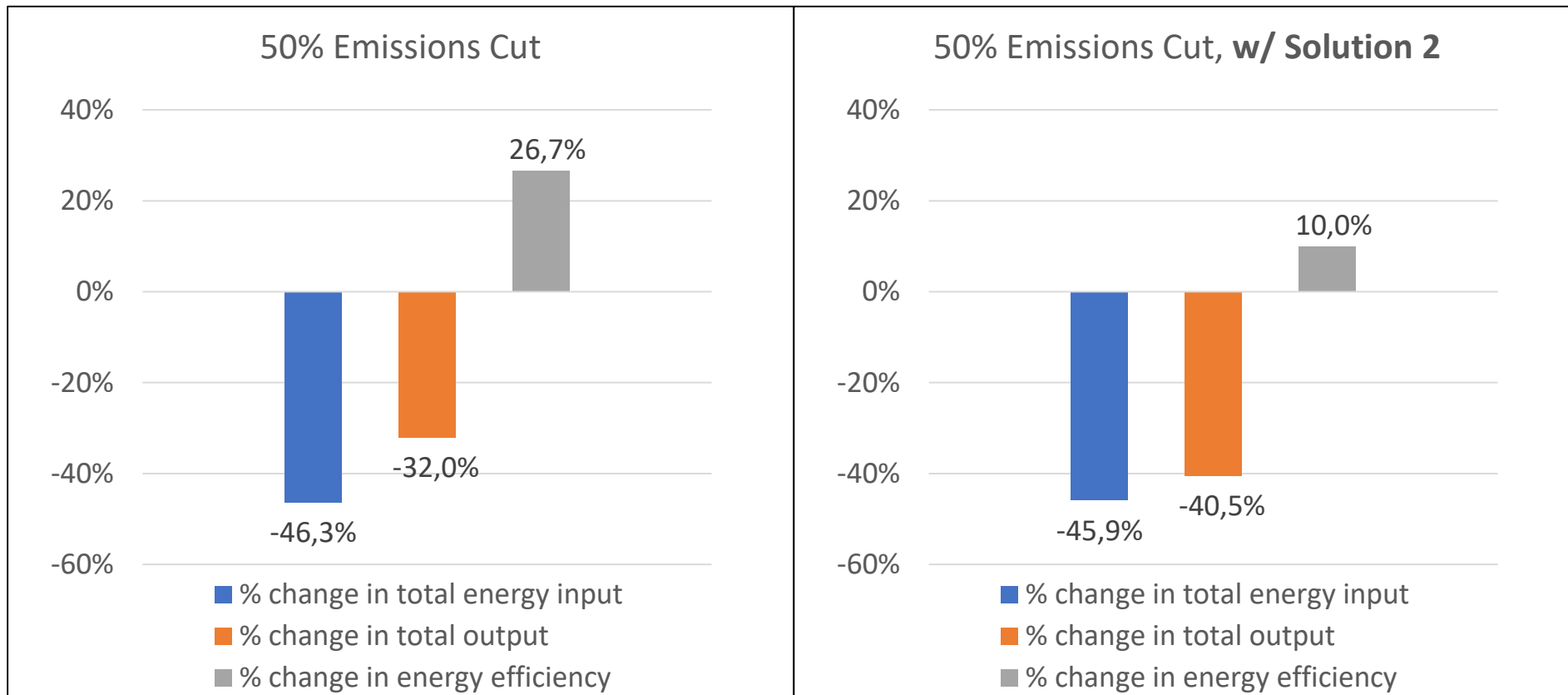
$$TX \cdot V_X \cdot P_X \cdot X = -SF \cdot (V_{GX} \cdot P_{GX} \cdot GX + V_{OX} \cdot P_{OX} \cdot OX + V_{AX} \cdot P_{AX} \cdot AX)$$

- $TX$  is an output tax rate for sector X
- $V_X$  is the baseline value of sector X output
- $P_X$  is the price index of sector X output
- $X$  is the output index for sector X
- $SF$  is an input subsidy rate for fuel inputs to sector X
- $V_{GX}$ ,  $V_{OX}$  and  $V_{AX}$  are the baseline values of G, O, and A fuel inputs to sector X
- $P_{GX}$ ,  $P_{OX}$  and  $P_{AX}$  are the price indices of G, O, and A fuel inputs to sector X
- $GX$ ,  $OX$ , and  $AX$  are the consumption indices of G, O, and A fuel inputs to sector X

## The Energy Efficiency Constraint changes Fuel Prices and Fuel Use



## The Energy Efficiency Constraint affects Input and Output Levels



## Solution 2: Energy Efficiency Changes Issue Resolved...

### 1. The Substitution Pattern

Consider two fossil fuels.

A fossil fuel with a lower energy-related emissions coefficient can have a higher value-related emissions coefficient – if its energy price is higher.

Under carbon pricing, it therefore incurs a higher penalty. Consequently, its usage in a production function declines more.

### 2. Energy Efficiency Changes



Inter-fuel substitution in a production function can inadvertently change energy use levels in physical units. Energy efficiency of production is therefore more likely to get improved beyond physically realistic measures.

## Solution 2: Discussion

- Introducing the energy efficiency constraint **requires** only **minimal revisions**.
- Nevertheless, the energy efficiency constraint deals with the issue in an **aggregate** manner:
  - Substitution between fossil fuels and electricity likely includes greater efficiency potentials than substitution among fossil fuels themselves. Such **fuel-specific differentiations are not considered** in the efficiency constraint.
  - The efficiency constraint **not only restricts efficiency improvement resulting from the inter-fuel-substitution itself**, but affects the overall efficiency improvement, which can also be induced by substitution between fuels and other inputs like capital.
  - The upper efficiency bound should be carefully set such that it will not rule out higher efficiency potential. For example, in a dynamic model, it can be increased over time.
- Future research may find ways to more precisely **constrain efficiency gains resulting purely from the substitution among fossil fuels**. However, our attempts with more specific formulations so far caused difficulties in solution finding.

**Thank You for Your attention!**

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**Literature**

# Literature

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Link to the paper associated with this presentation:

[https://www.gtap.agecon.purdue.edu/resources/res\\_display.asp?RecordID=7196](https://www.gtap.agecon.purdue.edu/resources/res_display.asp?RecordID=7196)