

Combined impacts of food demand and climate change on land and water use: an integrated environmental-economic modelling approach

Hermann Lotze-Campen^a, Christoph Müller^{a,b}, Alberte Bondeau^a, Pascale Smith^c, Wolfgang Lucht^a

^aPotsdam Institute for Climate Impact Research (PIK), 14412 Potsdam, Germany

^bMax Planck Institute for Meteorology, 20146 Hamburg, Germany

^cLaboratoire des Sciences du Climat et l'Environnement (LSCE), Gif-sur-Yvette, France

Abstract: In the coming decades, world agricultural production systems will face serious challenges. Population growth, economic development, and lifestyle changes towards rich-country dietary patterns will lead to considerable increases in global food demand. Moreover, rising demands for renewable, biomass-based energy products as well as land to be set aside for nature conservation and biodiversity protection may restrict the area available for food production. On the biophysical side, global climate change will affect production conditions, for better or worse depending on regional characteristics. Moreover, the future path of long-term productivity growth in agriculture to adapt to these changes is subject to considerable uncertainty.

In order to simulate these combined effects consistently and in a spatially explicit way, we have linked the Lund-Potsdam-Jena Dynamic Global Vegetation Model (LPJ) with a "Management model of Agricultural Production and its Impact on the Environment" (MAgPIE). LPJ simulates the major biogeochemical features of plant growth and represents the global biosphere with a spatial resolution of 0.5 degree, which is equivalent to a grid size of about 50 by 50 km. LPJ provides potential yields for 13 major crop types, depending on soil conditions, climate and precipitation. MAgPIE is designed as a programming model covering the most important agricultural crop and livestock production types worldwide. It takes regional economic conditions (eg food demand, cost structures) as well as LPJ-derived biophysical constraints (eg potential crop yields, water availability) into account and derives specific land use patterns for each grid cell. These land use patterns are fed back into LPJ in order to derive biophysical impacts of different land use scenarios. One major objective of this modelling exercise is to assess under which economic and climate conditions regional water constraints may become binding.

A prototype of the coupled modelling system has already been applied to a small sample region. In this paper we also describe a global version of the land use model, covering 10 economic regions and international trade. Input data for regional cost structures and net-trade flows are taken from FAO statistics and the GTAP database.

Keywords: Integrated modelling; agricultural production; land use; water use; climate change

1. Agriculture as a crucial link between society and nature

Agricultural production interacts more closely than most other human activities with socio-economic and environmental conditions. In economic terms the agricultural sector is losing importance over time. The share of agriculture in GDP and labour force is now below five percent in most industrialised countries. These trends occur despite wide-ranging government interventions to achieve the contrary. From an environmental point of view, however, agriculture is of key importance in rich and poor countries alike. On a global scale, agricultural production accounts for about 40 percent of total land use, it uses about 70 percent of all freshwater withdrawals, affects nutrient cycles and the climate, and it is the most important driver of biodiversity loss. At the same time, environmental changes strongly influence agricultural productivity [Kendall and Pimentel, 1994]. Understanding the links between food consumption, agricultural production and related environmental impacts is challenging, as socio-economic and environmental driving forces and impacts occur at different spatial, temporal and thematic scales. We present a coupled modelling framework as a tool for an integrated environmental-economic analysis of the food system across different scales. While our scope is global in principle, for the purpose of demonstrating the viability of our concept we chose Germany as a pilot sample region.

2. Agricultural challenges in the 21st century

Whether food production will keep pace with the demand for improved diets for a rapidly growing world population is still under debate. Optimists note relatively low average crop yields, inefficiencies throughout the food production and consumption chain, and the ample reserves of potential arable land in many developing countries. Sounder government policies, wider application of green revolution technology, reduced inefficiencies, upgraded rural infrastructure, and greater investments in human resources and research will make much larger harvests possible and no insurmountable environmental constraints are foreseen [Alexandratos, 1999]. Pessimists point at many signs of environmental stress and increasing difficulties encountered in expanding agricultural land, water supply and crop yields, and in controlling pests. Large expansion of agricultural output may not be feasible and it seems doubtful that current levels of crop production can be sustained in a number of countries. With global warming the prospects for increased food production would become even less favourable than they are at present [Kendall and Pimentel, 1994].

World population will probably grow to about 10 billion people by the year 2100, with a median projection at 8.8 billion for the year 2050 [Lutz et al., 2001]. As income rises, people

tend to consume more calories in total, and the share of animal calories increases, especially the consumption of animal fats. Global meat consumption can be expected to rise by up to 3 percent annually over the next decades, due to a combination of population growth, growth in per-capita income and a high income elasticity of meat demand. Average global meat consumption per capita could increase from 32.6 kg/year now to 44-54 kg/year in 2030 [Keyzer et al., 2001].

Even at conservatively reduced growth rates in crop yields, global food supply may still outpace demand up to 2020 and real prices for agricultural commodities are likely to continue to fall [Rosegrant and Ringler, 1997]. However, the assumption of exponential growth paths instead of logistic curves has been questioned for projections in the very long run [Harris and Kennedy, 1999]. The potential of biotechnology and genetic engineering for accelerating agricultural productivity growth remains unclear and subject to a strong public debate. Some initial trials show positive effects, but environmental consequences have to be further investigated and widespread social acceptance remains questionable [Qaim and Zilberman, 2003].

The total land area available for agricultural production is determined, apart from biophysical conditions, by land requirements for other economic and environmental purposes. Infrastructure development and urbanisation may reduce agricultural areas around the major population centres. In the course of a major energy transition a significant demand for bio-fuel production may arise, either from fast growing forests or from agricultural crops. Moreover, a certain share of land may have to be set aside for biodiversity protection [Sands and Leimbach, 2003].

More intensive production systems may lead to land degradation. This is a very important issue in some geographic regions and could become a serious threat to global food supply [Döös, 2002]. In order to assure sufficient nutrient supply for more intensive production on a global scale, the demand for fertilizer will rise. Especially nitrogen requirements will strongly increase up to 50 percent above current consumption by 2050. The consequences for sensitive environmental systems and the nitrogen cycle remain unclear [Gilland, 2002].

Water may pose the most serious limitation to future global food supplies. Irrigated areas account for nearly two-thirds of world rice and wheat production. Rising irrigation output per unit of land and water is essential to feed growing populations. Since the development of traditional irrigation and water supplies is increasingly expensive and new sources like desalination are not expected to play a major role soon, water savings at every level are absolutely necessary. Crop output per unit of evaporative loss has to be increased and water pollution has

to be reduced. However, the size of potential water savings in agricultural irrigation systems is unclear. While specific water uses can be made more efficient through better technology, the potential overall savings in many river basins are probably much smaller, because much of the water currently lost from irrigation systems is re-used elsewhere. Increasing water demand from households and industry will further exacerbate the challenge [Rosegrant and Cai, 2003]. The specific water requirements for various agricultural products differ widely, from less than 200 litres per kg output for potatoes, sugar beets or vegetables, to more than 1000 litres per kg output for wheat and rice [Barthélemy et al., 1993]. A typical diet with meat consumption at American levels requires about 5400 litres of water for crop evapotranspiration, while a comparable vegetarian diet requires only about half the amount. The future global challenge with respect to agriculture and water implies that over the next 25 years food production has to be increased by about 40 percent while reducing the renewable water resources used in agriculture by 10-20 percent [Rijsberman, 2001].

An additional constraint to agricultural production in the second half of the 21st century is global climate change. A rise in atmospheric CO₂-levels and a corresponding rise in global temperatures will not only affect plant growth and yields, but also alter the regional patterns of precipitation and water availability as well as land erosion and fertility. So far, sensitivity studies of world agriculture to potential climate changes have indicated that global warming may have only a small overall impact on world food production because reduced production and yields in some areas are offset by increases in others. However, regional impacts vary quite significantly, with tropical regions especially suffering from droughts. Moreover, the combined effects of various changes are still highly uncertain [IPCC, 2001].

3. An integrated environmental-economic modelling framework

The impacts of agricultural production on natural conditions strongly depend on specific local conditions. Changes in water or nutrient cycles are related to soil conditions, terrain type and local climate conditions. Hence it is necessary to link economic conditions of agricultural production to the place-specific biophysical conditions, in order to better understand their interactions. The key challenge with respect to modelling is to link place-specific models of agricultural production and land use with models representing important elements of the biosphere and hydrology. Our starting point for improving the understanding of society-biosphere interactions is the extension of one of the most prominent models of the global biosphere – the Lund-Potsdam-Jena (LPJ) Dynamic Global Vegetation Model. We suggest a way to integrate human activities into LPJ and come up with a coupled climate-biosphere-

economy modelling framework, including the water cycle (Figure 1). This is an important improvement on existing research, as LPJ endogenously models the dynamic linkages between climate and soil conditions, water availability and plant growth. It can be used to define plausible biophysical constraints to agricultural production and other human activities [Sitch et al., 2003].

The global version of LPJ has a spatial resolution of 0.5 degrees, which is equivalent to a grid size of about 50x50 km at the equator. The fundamental entity simulated in LPJ is the average individual of a plant-functional type (PFT). This concept provides a simple way for process acting at the level of the plant individual to be scaled up to the “population” over a grid cell. The grid cell is treated as a mosaic divided into fractional coverages of PFTs and bare ground. LPJ simulates the global terrestrial carbon pool sizes and fluxes, and captures the biogeographical distribution of Earth’s major biomes. In addition to the PFTs representing natural vegetation, 13 crop functional types (CFTs) have been implemented in order to simulate potential agricultural production. These CFTs represent 8 classes of agricultural crops, e.g. temperate cereals (wheat), tropical cereals (millet), rice, maize, pulses (lentil), oil crops (sunflower, soybean, groundnut, rapeseed), roots and tubers (sugar beet, manioc), and fodder crops (C3 and C4 grass). Input data required by LPJ are monthly fields of mean temperature, precipitation and cloud cover. Standard LPJ outputs include changes in net primary production and different fractions of biomass, changes in carbon pools and water balances. Under given climate conditions, soil type and water supply, the CFTs generate crop yields in terms of above-ground biomass as well as harvested organs. LPJ is written in C++ code.

The socio-economic part of the coupled modelling system, MAgPIE, is a linear-programming model with a focus on agricultural production, land and water use. The goal function is to produce a required amount of food energy at minimal costs. Food demand is defined for an exogenously given population in three energy categories (crops, meat, milk). Energy can be produced with 8 cropping activities (bread grain, feed grain, oil crops, sugar crops, roots/tubers/pulses, vegetables/fruits/nuts, rice, fodder crops) and 3 livestock activities (ruminant meat, non-ruminant meat, milk). Variable inputs of production are labour, chemicals, and other capital (measured in US\$). Crop land, pasture and water are fixed inputs in limited supply, measured in physical units. MAgPIE is written in Python code. Currently the two models are coupled offline by exchanging text files. Later, we will use the typed data transfer (TDT) protocol.

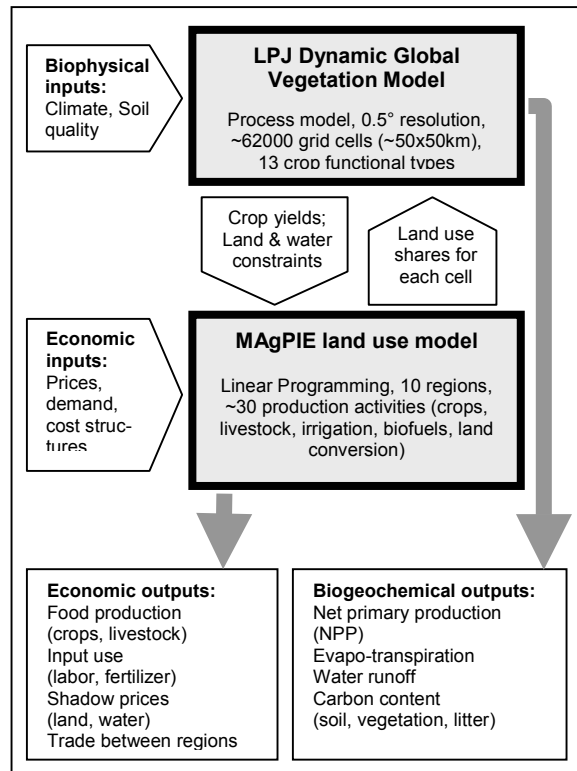


Figure 1: The coupled modelling structure

4. Illustrative application of the modelling framework for a sample region

So far the modelling framework has been applied to one pilot region without external trade. The regional demand for intermediate inputs like feed grain and green fodder has to be met by regional production. Water supply is currently defined purely by precipitation inflows. We abstract from groundwater reservoirs, lakes or other water storages. Water demand from production activities is calculated using fixed coefficients per unit of crop or livestock output. In order to keep the cropping mix within plausible bounds we introduce rotational constraints. Average production costs are based on data from FAO and the Global Trade Analysis Project. MAgPIE output includes the shares of different crops in total food energy production and land use, purchases of variable inputs, and shadow prices for fixed inputs and other constraints. The generation of shadow prices is especially useful, as it facilitates the assignment of internal use values to factors of production for which no proper markets and, hence, no observable prices exist.

Several challenges have to be overcome in coupling the two models. First, thematic scales have to be matched. CFTs in LPJ, based on plant-physiological properties, have to be

matched with groups of crops which provide a similar type of output for human consumption. Oil crops, for instance, comprise a wide variety of plant species (e.g. rapeseed, groundnuts, sunflowers, oil palms etc.), but they all deliver similar types of oil, which are almost perfectly substitutable in the processing of agricultural products. Second, temporal scales have to be made consistent. While LPJ is usually run over a period up to the year 2100, most economic forecasts do not go beyond 2020, as changes in technology and input use are very hard to predict in the longer run. Third, we have to bridge the gap between the national or regional scale in MAgPIE and the 50x50km-grid scale in LPJ. While it is hardly possible to model economic activity on a 0.5-degree-grid for a larger region, it does not make much sense either to model environmental impacts on the aggregated national level. In order to bridge this gap, we grouped LPJ cells into a small number of "productivity zones", according to the normalised level of crop yields in each grid cell.

For our sample case of Germany we have 185 grid cells grouped in 6 different zones. Effectively this means, that MAgPIE can choose among 8 cropping activities and 3 livestock activities in 6 different zones, yielding in total 66 different production activities in the given region. We can distinguish between constraints to be fulfilled in each zone and constraints to be fulfilled at the regional level. This introduces aspects of trade between zones. For instance, feed grain produced in any zone is pooled across all zones and can be used in the whole region, as long as the overall balance is maintained. In contrast, green fodder has to be used locally and, hence, we impose a separate constraint for each zone. Land and water are also constrained in each zone. Having separate constraints for different zones implies that MAgPIE generates different land use shares and shadow prices for each zone.

Our reference scenario in this paper is the situation in Germany in the year 2000, defined by climate conditions, yields, the fraction of arable land and pasture in total area, and cost structures in agricultural production at this point in time. Then we look at 4 different drivers of agricultural production: a change in climate conditions as predicted for the year 2020 ("environmental change"); an increase in total food energy demand by 10 % ("income change"); a decrease in meat energy demand by 10 % ("lifestyle change"); a decrease in available crop land by 10 % ("demand for land from energy sector"). The different impacts of these drivers can be analysed separately, but here we only present the combined results.

In step 1 of our analysis we run LPJ separately with each CFT in order to define potential yields for each grid cell. Figure 2 shows yield distributions for "temperate cereals" in 2000. The map reveals significant variation in yields across the region. Currently, yields in LPJ

strongly depend on precipitation and less on soil conditions. This is partly due to the rather crude soil classification in the FAO soil data set used in LPJ.

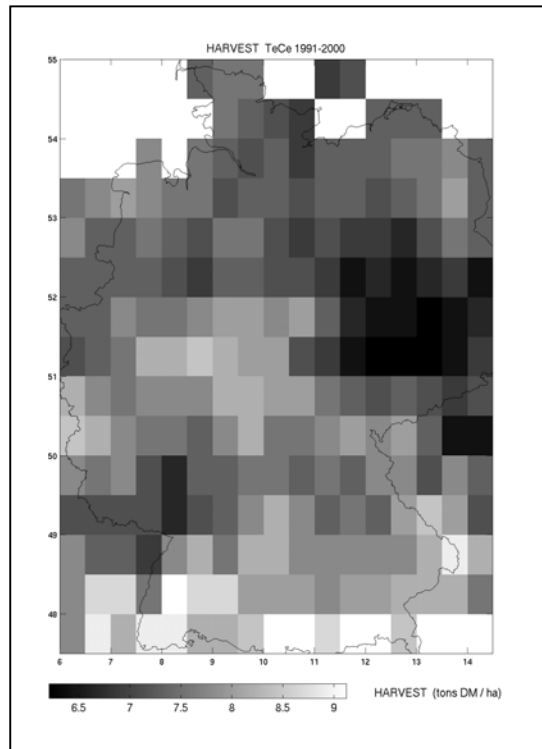


Figure 2: Regional distribution of potential cereal yields in Germany in 2000 (LPJ calculations)

In step 2 we use normalised yields for cereals and maize as the most important crops in terms of land use share, in order to define 6 productivity zones. In step 3 of our analysis these characteristics of zones and yields are implemented in MAgPIE, and in step 4 agricultural production and resource use are optimised for the sample region. Total food energy demand for Germany is calculated by multiplying a population of 82 million by an average daily food *availability* of 3411 kcal or 14272 MJ (according to the FAO food balance sheets). More precise data on effective food *intake* are not available. The shares in total food energy consumption are 69 % for plant-based energy, 17 % for meat-based energy, and 14 % for milk-based energy. With the current specification of MAgPIE, in the reference situation total food demand in Germany can be met, the self-sufficiency ratio is about 110 %. Under these conditions the model leaves in the optimised solution about 10 % of crop land and 9 % of pasture unused (Table 1).

Table 1: Average land use shares for Germany under various scenarios
(MAGPIE calculations, %)

	Year 2000	Climate 2020	Demand increase	Reduced meat	Reduced crop land	Combined
Bread grain	16	11	11	21	11	13
Feed grain	50	53	55	45	55	52
Rapeseed	14	15	19	9	22	18
Sugar beet	0	0	3	0	1	0
Silage maize	10	11	12	10	11	12
Unused cropland	10	9	0	15	0	5
Unused pasture	9	1	4	9	10	1

The shares of rapeseed and sugar beet in total land use are currently underestimated in the model compared to observed data. Climate change, a demand increase and reduced crop land tend to shift land use towards more feed grain and high-energy crops like sugar beets and rapeseed. Reduced meat consumption leaves room for more bread grain production. In the combined scenario some of these effects eliminate each other. The resulting shadow prices for the combined scenario show considerable variation between zones, as e.g. crop land and pasture are scarce in some zones, but not in all (Table 2). Water is not a binding constraint in any zone, i.e. the shadow price is always zero. The rotational constraint on cereals is binding in all zones, except zone 2, which is rather small in this scenario.

Table 2: Regional and zone-specific shadow prices in combined scenario
(MAGPIE calculations, US\$)

<i>Zone</i>	<i>1</i>	<i>2</i>	<i>3</i>	<i>4</i>	<i>5</i>	<i>6</i>
Regional constraints						
Crop energy				17		
Meat energy				852		
Milk energy				526		
Feed grain balance				18		
Zone-specific constraints						
Fodder balance	14	127	12	14	11	13
Crop land	612	1288	319	213	106	0
Pasture	2800	0	2848	2819	2875	2841
Rotation cereals	291	0	319	310	301	272
Water	0	0	0	0	0	0

The fact that pasture has a higher shadow price than crop land is implausible and indicates that livestock production activities in MAGPIE have to be refined. In step 5 the land use patterns for each zone are implemented in LPJ and in step 6 the impacts on net primary produc-

tion (NPP), carbon and water balances are calculated. Figure 3 shows the difference in NPP in the combined scenario compared to the reference situation in 2000. Changes in NPP, water and carbon balances are dominated by climate impacts in our current scenarios, as these affect both crops and forest. Forest and unused land account for about 40 percent of the total area in Germany. It will be subject to future research, whether different cropping patterns have a significant impact on environmental indicators in other regions.

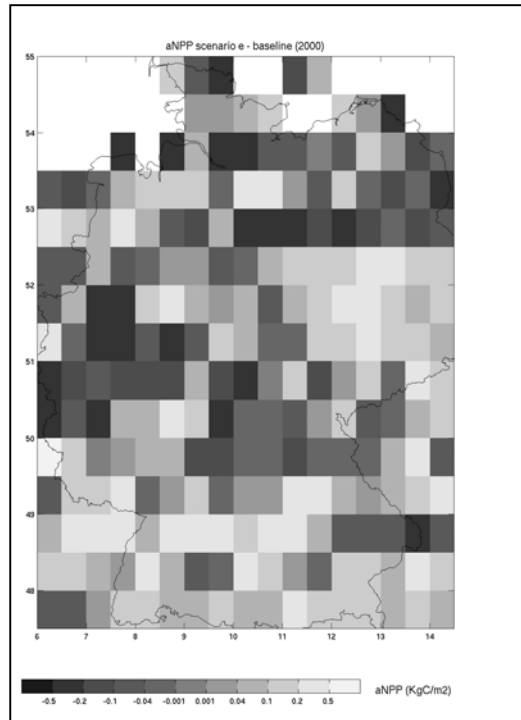


Figure 3: Regional changes in Net Primary Production (NPP), combined scenario compared to reference (LPJ calculations)

5. Global version of the modelling framework

A global version of the coupled MAGPIE-LPJ model is currently under development. First results are expected soon. The economic part of the model covers 10 regions on a global scale: North America, Latin America, Europe, Middle East/North Africa, Sub-Saharan Africa, Newly Independent States of the Former Soviet Union, China, South Asia including India, Japan/Australia/New Zealand, and Southeast Asia. In order to keep the model size at reasonable limits and relate it closely to the question of food production and water scarcity, the LPJ cells have been grouped into 575 river basins on a global scale. Trade between regions can be simulated using different sets of regional and global constraints in the programming model. Land conversion activities have been included, in order to simulate potential expansion of

agricultural land in specific locations. Potential crop yields and related crop water requirements have been calculated up to the year 2050 with LPJ, taking effects of climate change into account. Plausible scenarios on population growth, income growth and dietary structures will be fed into the programming model, from which specific land use shares and shadow prices will be derived for each river basin.

6. Conclusions and outlook

With the preceding analysis we have shown how a grid-based dynamic global vegetation model and a non-spatial economic optimisation model can be coupled. The preliminary results show the viability of the concept. This modelling approach can in principle be run on the small scale of a single grid cell or even a single farm as well as on the global scale. Hence, it provides the opportunity for consistent spatial aggregation and dis-aggregation and nested modelling structures. It can also be coupled to a food demand model or an economy-wide model, in order to make markets and prices for outputs and inputs endogenous. Here we will build upon recent developments in the area of model coupling and meta-optimisation at PIK [Jaeger et al., 2002].

However, several caveats apply. The 0.5-degree-resolution of the current version of LPJ may not be appropriate for all applications, especially when it is coupled with economic models. It may be necessary to develop a flexible grid structure depending on the question at hand. E.g. in the case of water related questions a spatial aggregation related to river basins may be more appropriate. In order to simplify the computation, especially when long-term dynamics are to be considered, the structure of LPJ also calls for a limitation of the number of grid cells.

Crop yields and crop growth functions in LPJ have to be further evaluated. The specification of production activities in MAgPIE is rather preliminary, especially the linkages between livestock and crop production, and water requirements by crops have to be refined. The linear-programming technique is powerful, flexible, and computationally very efficient. However, a non-linear programming approach is required to enable more complex structures of the biophysical constraints. In the case of water it would be useful to include stocks of natural resources to be managed over time.

The most challenging task will be the implementation of technological change, which is crucial in the very long run. Many aspects of water and nutrient cycles are only poorly monitored and not yet well understood, but they are strongly influenced by agricultural production tech-

nologies. Finally, the model results should be validated using satellite remote sensing and agricultural statistics.

7. References

- Alexandratos, N., World food and agriculture: Outlook for the medium and longer term, *Proceedings of the National Academy of Sciences of the United States of America*, 96 (11), 5908-5914, 1999.
- Barthélemy, F., D. Renault, and W. Wallender, Water for a sustainable human nutrition : inputs and resources analysis for arid areas, UC Davis Internal report, 1993.
- Bender, W., and M. Smith, Population, food, and nutrition, *Population Bulletin*, 51 (4), 2-47, 1997.
- Bender, W.H., How much food will we need in the 21st century?, *Environment*, 39 (2), 7-28, 1997.
- Döös, B.R., Population growth and loss of arable land, *Global Environmental Change-Human and Policy Dimensions*, 12 (4), 303-311, 2002.
- Gilland, B., World population and food supply - Can food production keep pace with population growth in the next half-century?, *Food Policy*, 27 (1), 47-63, 2002.
- Harris, J.M., and S. Kennedy, Carrying capacity in agriculture: global and regional issues, *Ecological Economics*, 29 (3), 443-461, 1999.
- Intergovernmental Panel on Climate Change (IPCC), Third Assessment Report - Climate Change 2001, 2001.
- Jaeger, C.C., M. Leimbach, C. Carraro, K. Hasselmann, J.C. Hourcade, A. Keeler, and R. Klein, Integrated assessment modeling: modules for cooperation, FEEM Working Paper 53-2002, 2002.
- Keyzer, M.A., M.D. Merbis, and I.F.P.W. Pavel, Can we feed the animals? Origins and Implications of rising meat demand, Centre for World Food Studies, Amsterdam, 2001.
- Kendall, H.W., and D. Pimentel, Constraints on the expansion of the global food supply, *Ambio*, 23 (3), 1994.
- Lutz, W., W. Sanderson, and S. Scherbov, The end of population growth, *Nature*, 412, 543-545, 2001.
- Qaim, M., and D. Zilberman, Yield effects of genetically modified crops in developing countries, *Science*, 299, 900-902, 2003.

- Rijsberman, F.R., Molden, D., Balancing water uses: water for food and water for nature, in *Thematic background paper to the International Conference on Freshwater*, Bonn, 2001.
- Rosegrant, M.W., and X. Cai, Global water demand and supply projections. Part 2: results and prospects to 2025, *Water International*, 27 (2), 170-182, 2003.
- Rosegrant, M.W., and C. Ringler, World food markets into the 21st century: environmental and resource constraints and policies, *Australian Journal of Agricultural and Resource Economics*, 41 (3), 401-428, 1997.
- Sands, R.D., and M. Leimbach, Modeling agriculture and land use in an integrated assessment framework, *Climatic Change*, 56, 185-210, 2003.
- Sitch, S., B. Smith, I.C. Prentice, A. Arneth, A. Bondeau, W. Cramer, J. Kaplan, S. Levis, W. Lucht, M. Sykes, K. Thonicke, and S. Venevski, Evaluation of ecosystem dynamics, plant geography and terrestrial carbon cycling in the LPJ Dynamic Vegetation Model, *Global Change Biology*, 9, 161-185, 2003.

Appendix: MAgPIE - Model description

Variables

<i>x</i>	level of activity (22 crops (ha), 3 livestock (ton), 2 irrigation (m ³), 2 land conversion (ha), 3 input purchases (US\$))
----------	--

Parameters

<i>c</i>	production costs per activity unit (US\$)
<i>d_food</i>	demand for food energy (GJ)
<i>d_fibr</i>	demand for fibre (ton)
<i>d_biof</i>	demand for biofuel energy (GJ)
<i>y_food</i>	food energy delivery (from crops and livestock) (GJ)
<i>y_fibr</i>	fibre delivery (from fibre crops) (ton)
<i>y_biof</i>	biofuel energy delivery (from agric. crops or forest) (GJ)
<i>y_feed</i>	feed energy delivery (from crops and residues) (GJ)
<i>y_fodd</i>	green fodder energy delivery (from crops) (GJ)
<i>y_land</i>	land delivery (i.e. from conversion activities) (ha)
<i>y_wat</i>	water delivery (i.e. from irrigation activities) (m ³)
<i>y_input</i>	variable input delivery (i.e. labour, chemicals, capital) (US\$)
<i>req_feed</i>	feed energy requirement (i.e. per ton of livestock output) (GJ)
<i>req_fodd</i>	green fodder energy requirement (i.e. per ton of livestock output) (GJ)
<i>req_land</i>	land requirements (i.e. cropland, pasture) (ha)
<i>req_wat</i>	water requirements (in different sub-seasons) (m ³)
<i>req_input</i>	variable input requirements (i.e. labour, chemicals, capital) (US\$)
<i>req_share</i>	area to be considered for rotational constraints (ha)
<i>land_const</i>	available land (cropland, pasture, non-agric.) (ha)
<i>wat_const</i>	available water from precipitation without irrigation (m ³)
<i>irri_const</i>	available water for irrigation, in addition to precipitation (m ³)
<i>max_share</i>	maximum crop share in average rotation (%)

Indices

- i number of economic regions (10)
 j number of LPJ-cells per region (total: 2188 at 3°x3° resolution)
 k number of activities (22 crops (kcr), 3 livestock (kli), 2 irrigation (kir), 2 land conversion (klc), 3 input purchases (kin))
 l number of food energy demand categories (10)
 m number of agricultural land types (3) (cropland, pasture, non-agri)
 n number of rotational constraints (10)
 t number of relevant sub-seasons for crop growth (2, i.e. early, late)

Goal function: Cost minimisation (Regional costs of production; for all i regions):

$$C_i = \sum_j \sum_k x_{i,j,k} * c_{i,k}$$

subject to:

Regional constraints (for all i regions): (Note: all k activities are included in all constraints, in order to reduce the number of indices; however, many of the parameter values may be zero)

Food energy demand (minimum constraint; for all l demand types):

$$\sum_j \sum_k x_{i,j,k,l} * y_food_{i,j,k,l} \geq d_food_{i,l}$$

Fibre demand (minimum constraint):

$$\sum_j \sum_k x_{i,j,k} * y_fibr_{i,j,k} \geq d_fibr_i$$

Biofuel demand (minimum constraint):

$$\sum_j \sum_k x_{i,j,k} * y_biof_{i,j,k} \geq d_biof_i$$

Feed energy balance (regional demand $\leq$ regional supply)

$$\sum_j \sum_k x_{i,j,k} * (req_feed_{i,k} - y_feed_{i,j,k}) \leq 0$$

Input purchase balances (regional demand $\leq$ regional supply; for all kin inputs)

$$\sum_j \sum_k x_{i,j,k} * (req_input_{i,k,kin} - y_input_{i,j,k,kin}) \leq 0$$

Cellular constraints (for all j cells):

Green fodder balance (cellular demand = cellular supply):

$$\sum_k x_{i,j,k} * (req_fodd_{i,k} - y_fodd_{i,j,k}) \leq 0$$

Land constraints (for all m land types):

$$\sum_k x_{i,j,k} * (req_land_{i,k,m} - y_land_{i,j,m}) \leq land_const_{i,j,m}$$

Land conversion constraint:

$$\sum_k x_{i,j,k} * y_land_{i,j,m} \leq land_const_{i,j,"non-agri"}$$

Rotational constraints (for all n constraint types):

$$\sum_k x_{i,j,k} * req_share_{i,k,n} \leq max_share_{i,n} * land_const_{i,j,"cropland"}$$

Water constraints (for all t sub-seasons):

$$\sum_k x_{i,j,k} * (req_wat_{i,k,t} - y_wat_{i,j,t}) \leq wat_const_{i,j,t}$$

Irrigation constraints (for all t sub-season):

$$\sum_k x_{i,j,k} * y_wat_{i,j,t} \leq irri_const_{i,j,t}$$